



# Neutron Reflectometry

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**Jun-04-2013**

**Canadian Neutron Scattering Summer School**



**National Research  
Council Canada**

**Conseil national  
de recherches Canada**

**Canada**

# Outlook

Application/advantages of neutron reflectometry

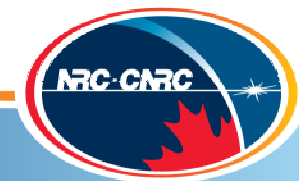
Theoretical background

Instrumental setup

Experiments:

- Photoactive azobenzene films
- Hydrogen absorption in Mg-based films

Supermirrors (non-polarizing and polarizing)



# What can be measured?

## Film thickness (2 – 200 nm):

swelling of polymer films due to water uptake  
film expansion during illumination of photoactive films  
film expansion during hydrogen absorption  
growth of oxide layer

## Scattering length density profile:

profile of absorbed gas/liquid  
interdiffusion  
magnetic structures  
magnetic field penetration into superconductors

In-plane structures on nm and  $\mu\text{m}$  scale

# Specific advantages of NR

Large penetration depth (for most materials):

Buried layers

In-situ measurements (cryostats, cryomagnets, high-pressure cells, furnaces)

High sensitivity to hydrogen:

Determine hydrogen profile in hydrogen storage materials

Change of contrast by using isotopes:

swelling of films during water (vapor or liquid) uptake ( $\text{H}_2\text{O}$  /  $\text{D}_2\text{O}$ )

expansion of films during hydrogen absorption ( $\text{H}_2$  /  $\text{D}_2$ )

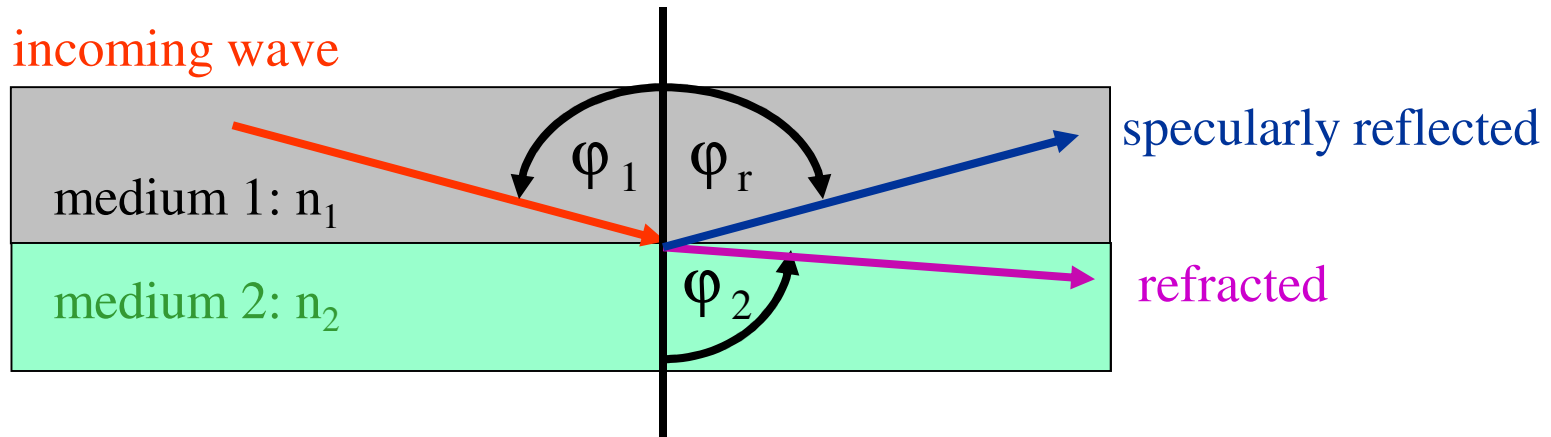
No diamagnetic background of substrate for ferromagnetic samples:

Determination of absolute magnetic moment

Spin and non-spin flip reflectivity:

Magnetization reversal, magnetic structure

# Reflection and Refraction



Physical origin:

*different* index of refraction for two media

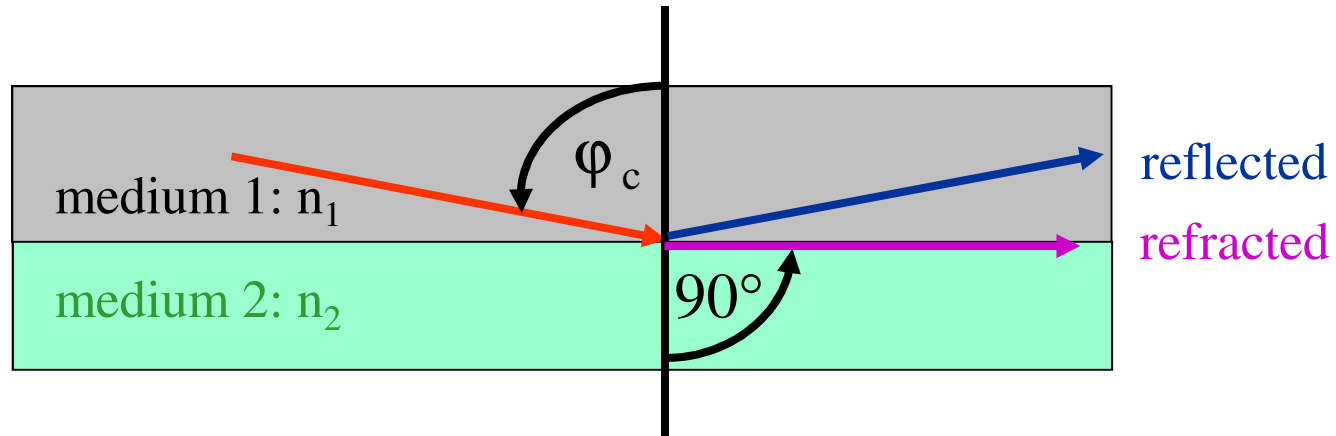
**Reflection:**

$$\varphi_r = \varphi_1$$

**Refraction: Snell's law**

$$n_1 \sin \varphi_1 = n_2 \sin \varphi_2$$

# The critical angle



**Critical angle:**  $n_1 \sin \varphi_1 = n_2 \sin 90^\circ \Rightarrow \sin \varphi_c = n_2 / n_1$

For  $\varphi_1 > \varphi_c$  : no refracted beam exists, only a reflected beam

**Total reflection** (100% reflectivity) occurs in the medium with the larger  $n$

# Index of refraction for light

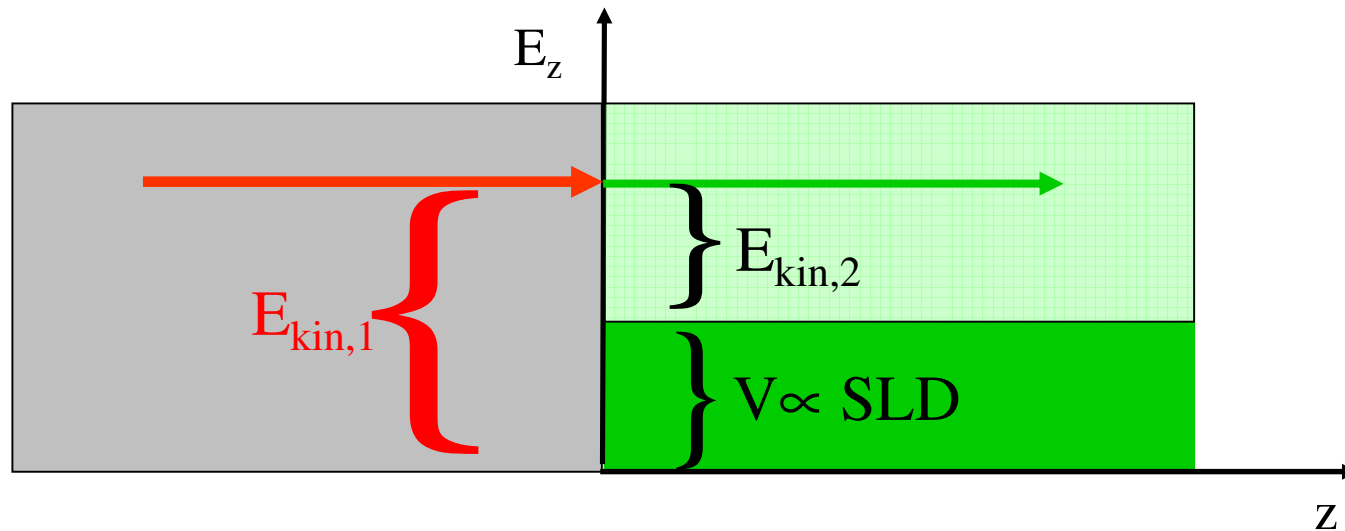
For light with  $\lambda = 656$  nm:

Material	n	$\varphi_c$ (for $n_2=1$ )
Vacuum	1.00	-
Water	1.33	48.8°
Quartz glass	1.46	43.2°
Benzene	1.50	41.8°

**Note: the index of refraction depends on the wavelength**

*What is the index of refraction for neutrons?*

# Index of refraction for neutrons



$$\frac{\hbar^2 k_1^2}{2m} = \frac{\hbar^2 k_2^2}{2m} + V \Rightarrow n = \frac{k_2}{k_1} = \sqrt{1 - \frac{2m \cdot V}{\hbar^2 k_1^2}} = \sqrt{1 - \frac{\lambda^2}{\pi} \rho b}$$

$m$ : neutron mass

$\lambda$ : neutron wavelength

$b$ : nuclear scattering length

$\rho$ : density of atoms

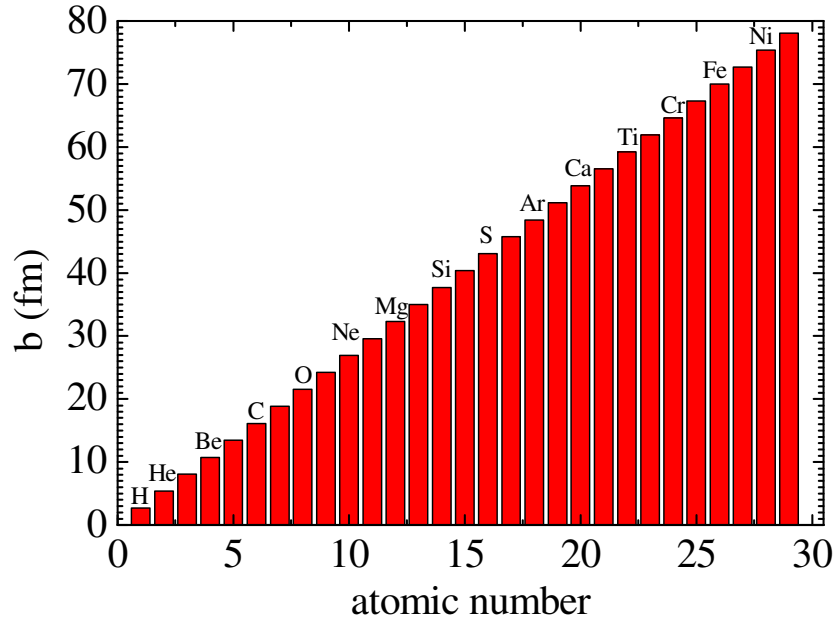
$\rho b$ : scattering length density (SLD)

Fermi's pseudopotential:  $V = \frac{2\pi\hbar^2}{m} \rho b$

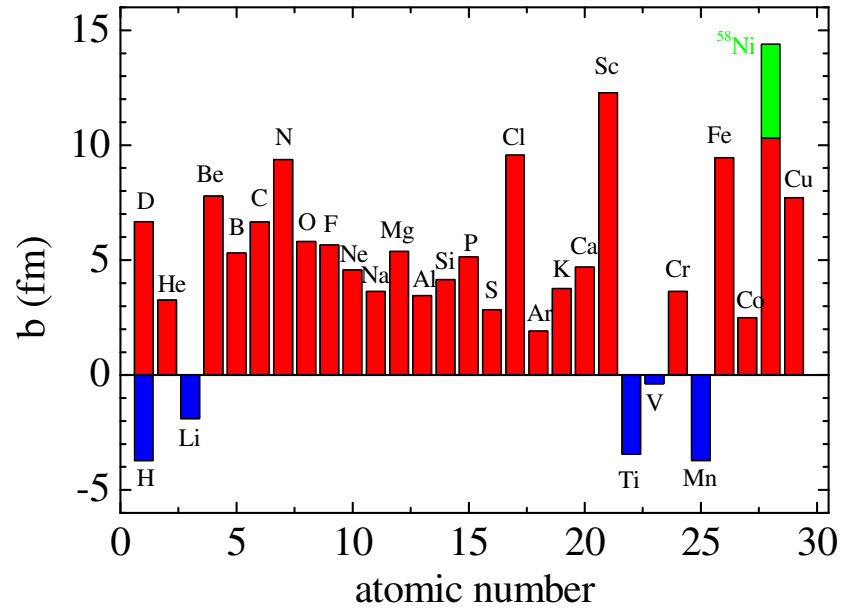


# Scattering length

X-rays



Neutrons



X-rays:  $b \propto Z$  (electron density)

Neutrons: no systematics

Important: not absolute number but contrast of SL  
X-rays and neutrons are complementary probes

# Index of refraction: some examples

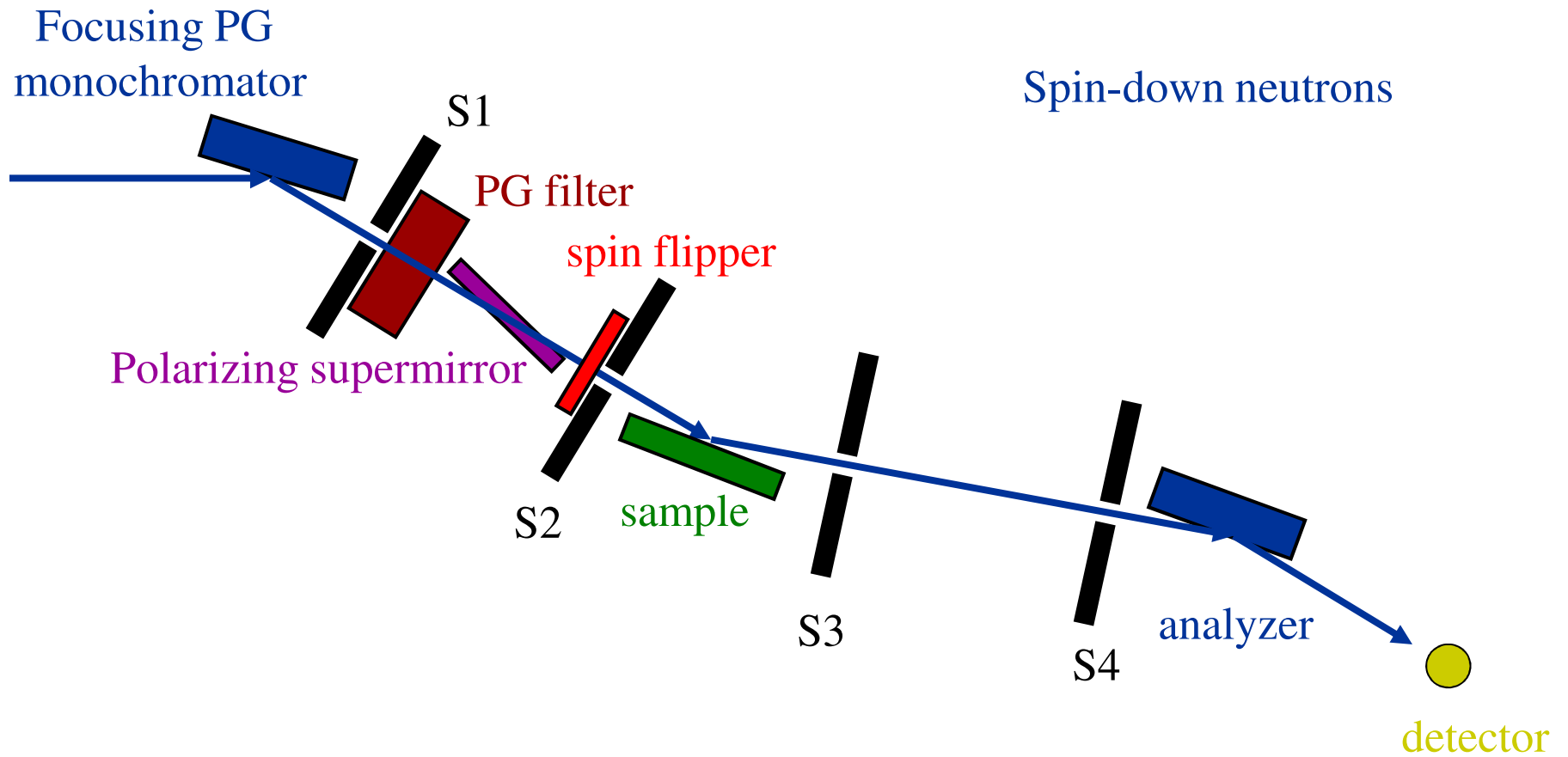
For neutrons with  $\lambda = 0.237$  nm:

Material	$n$	$\rho b$ ( $10^{-4}$ 1/nm <sup>2</sup> )
Vacuum	1.00	0
Water (H <sub>2</sub> O)	1.000001	-0.561
Si	0.999998	2.073
Quartz glass	0.999997	4.185
Heavy water (D <sub>2</sub> O)	0.999994	6.366
<sup>58</sup> Ni	0.999988	13.16

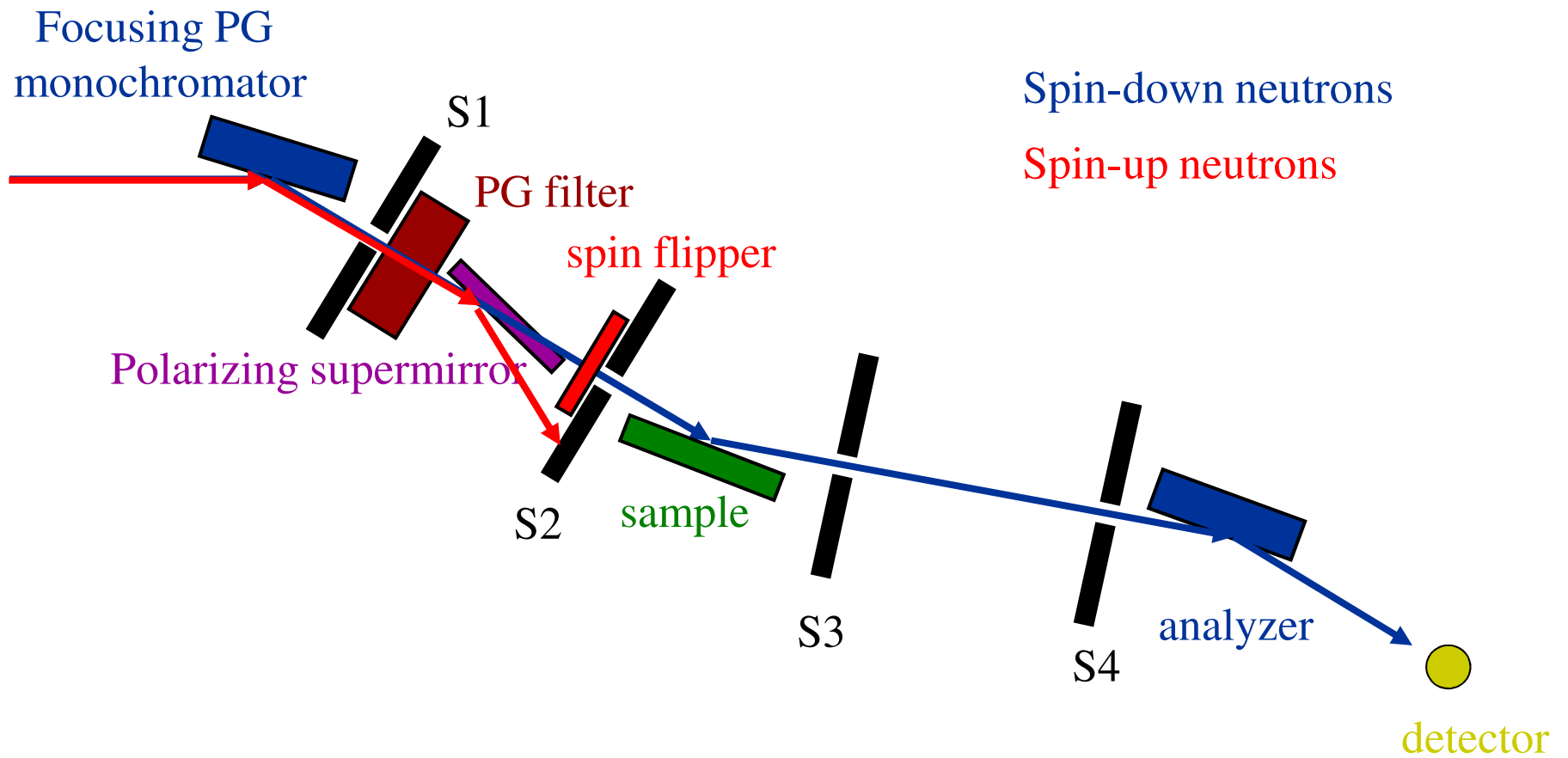
**Note:  $n \approx 1 - 10^{-5}$**

**The deviation of  $n_{\text{neutron}}$  from 1 is much smaller than for light, because the interaction of neutrons with matter is much weaker**

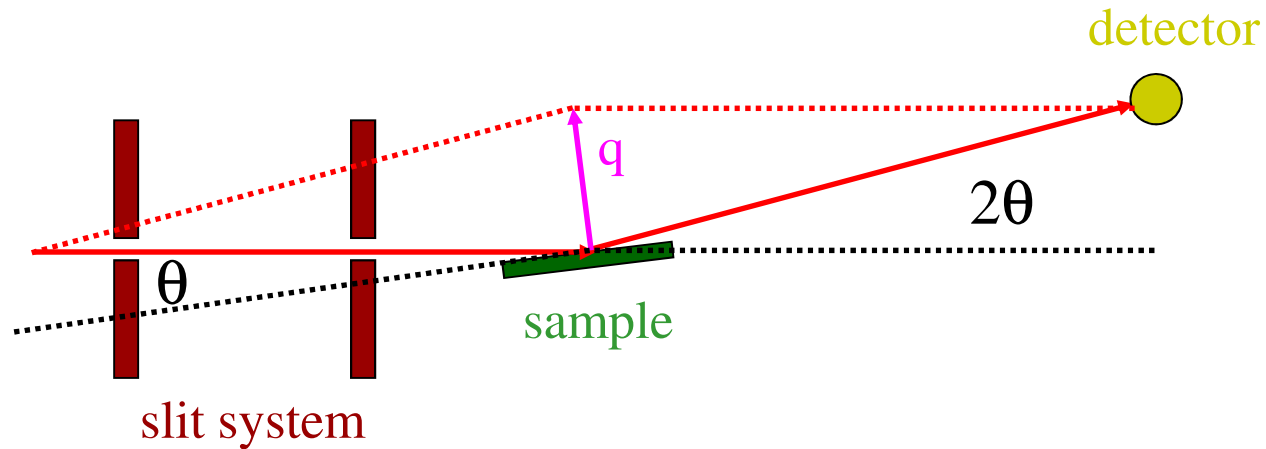
# Reflectometry setup on D3



# Reflectometry setup on D3



# The reflectometry experiment

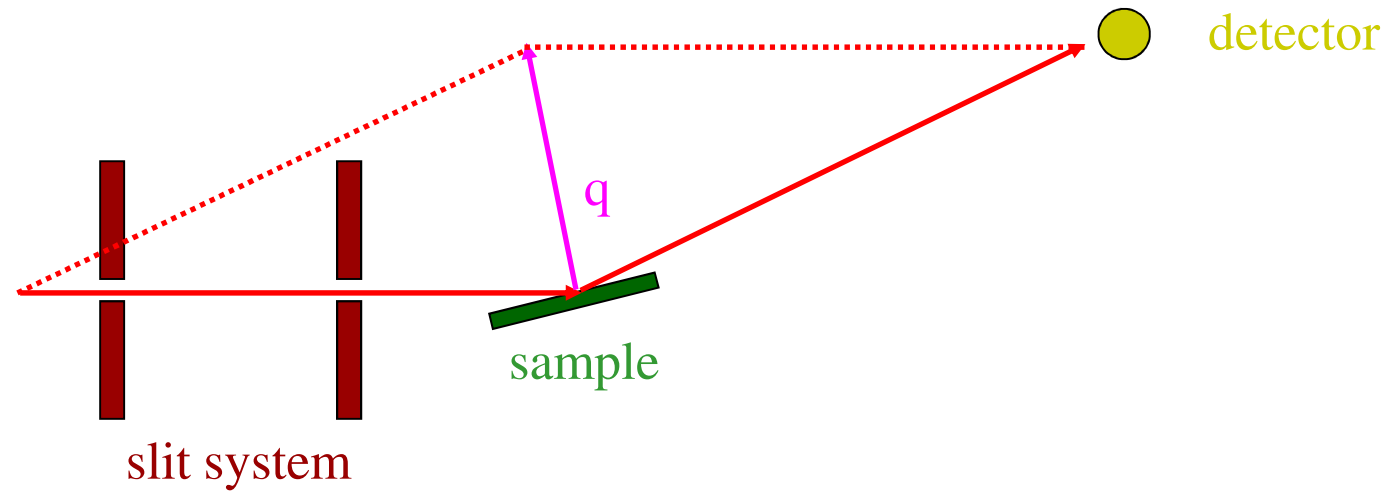


$\theta$ - $2\theta$  geometry:  
sample moves by  $\theta$   
detector moves by  $2\theta$

$$\vec{q} = \vec{k}_r - \vec{k}_i = \frac{4\pi}{\lambda} \sin \theta$$

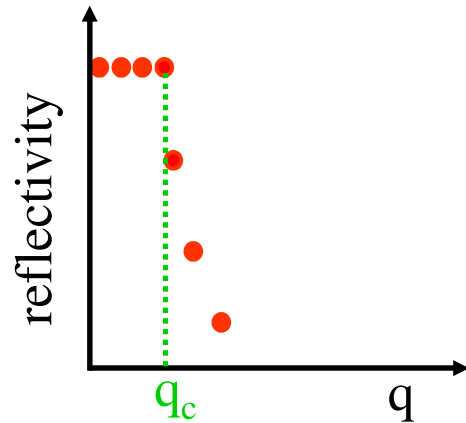
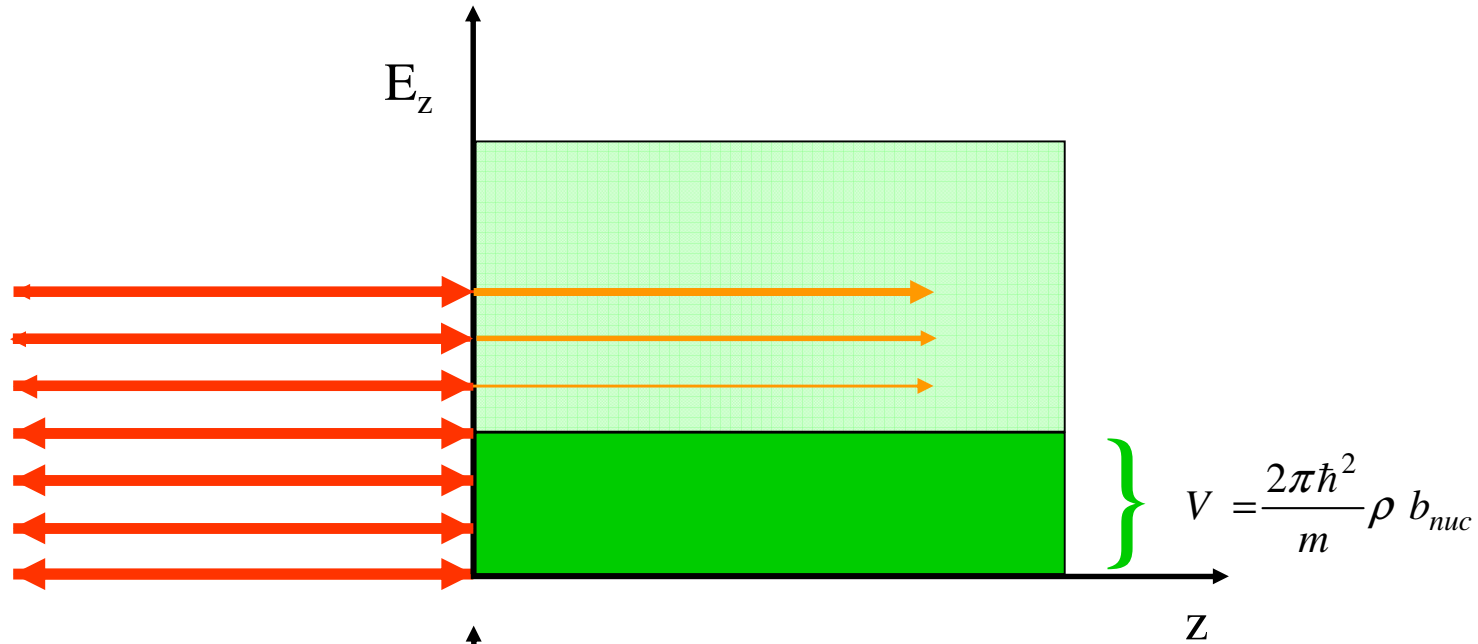
$q$ : scattering vector  
 $2\theta$ : scattering angle

# The reflectometry experiment



Reflectometry:  
Measuring the reflected intensity as a function of  $q$

# Visualization of a reflectivity curve

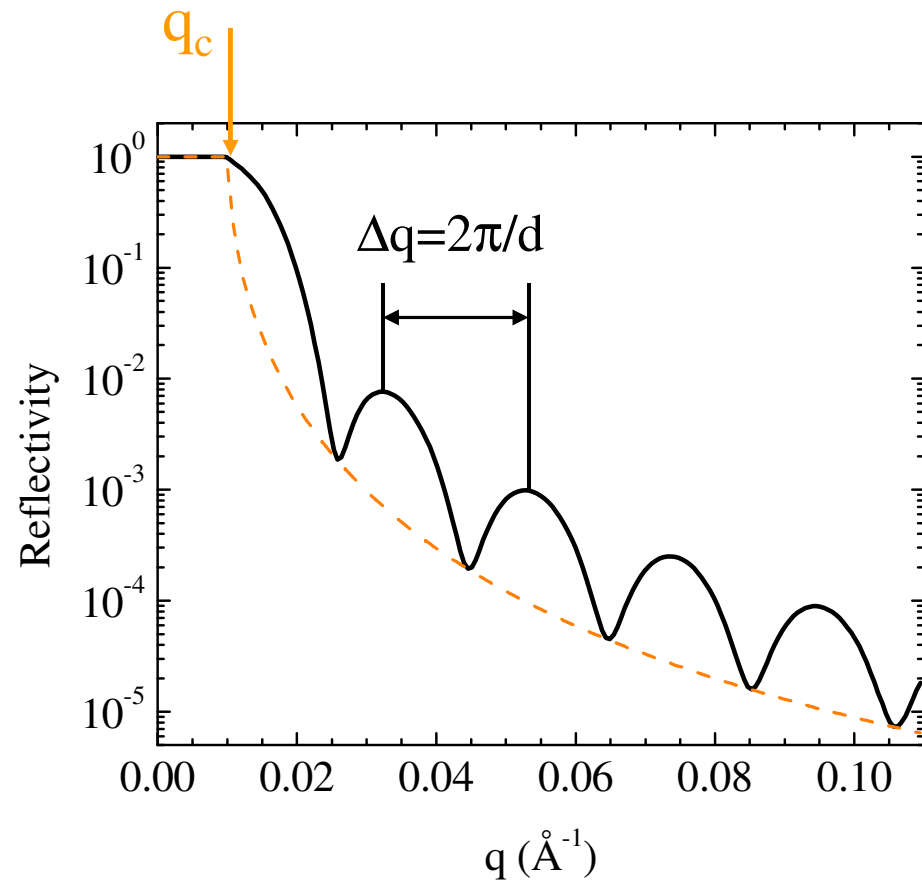
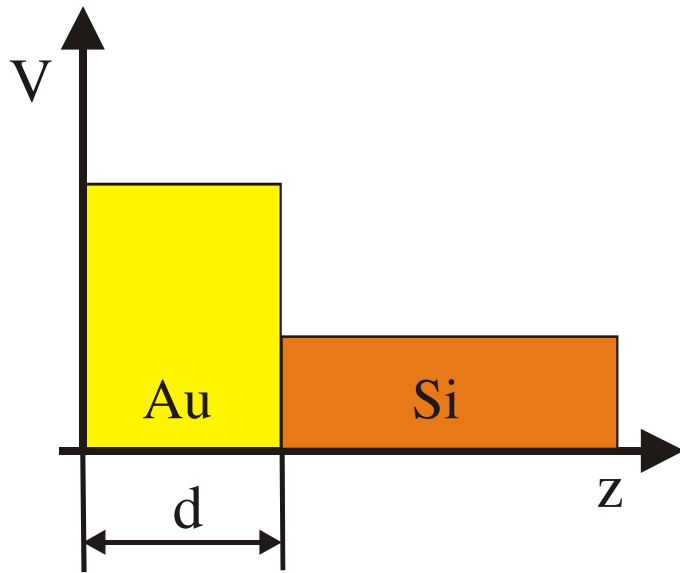


$$q_c = \frac{4\pi}{\lambda} \sin \theta_c \quad \theta_c = \lambda \sqrt{\frac{\rho b}{\pi}}$$

Si:  $\theta_c = 0.11^\circ$  (for  $\lambda = 2.37 \text{ \AA}$ )

$^{58}\text{Ni}$ :  $\theta_c = 0.28^\circ$  (for  $\lambda = 2.37 \text{ \AA}$ )

# Kiessig fringes



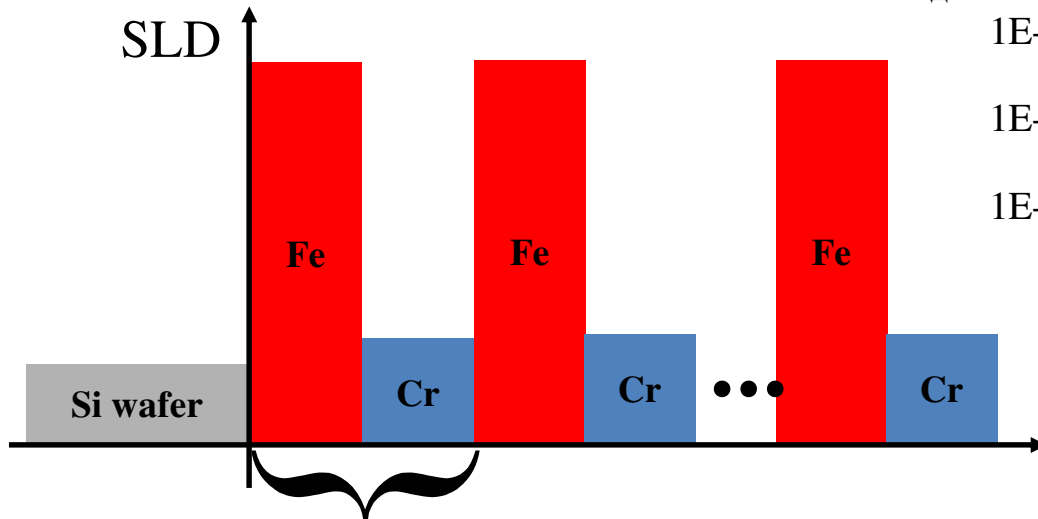
Oscillations due to total film thickness  
 $\Delta q \propto 1/d$



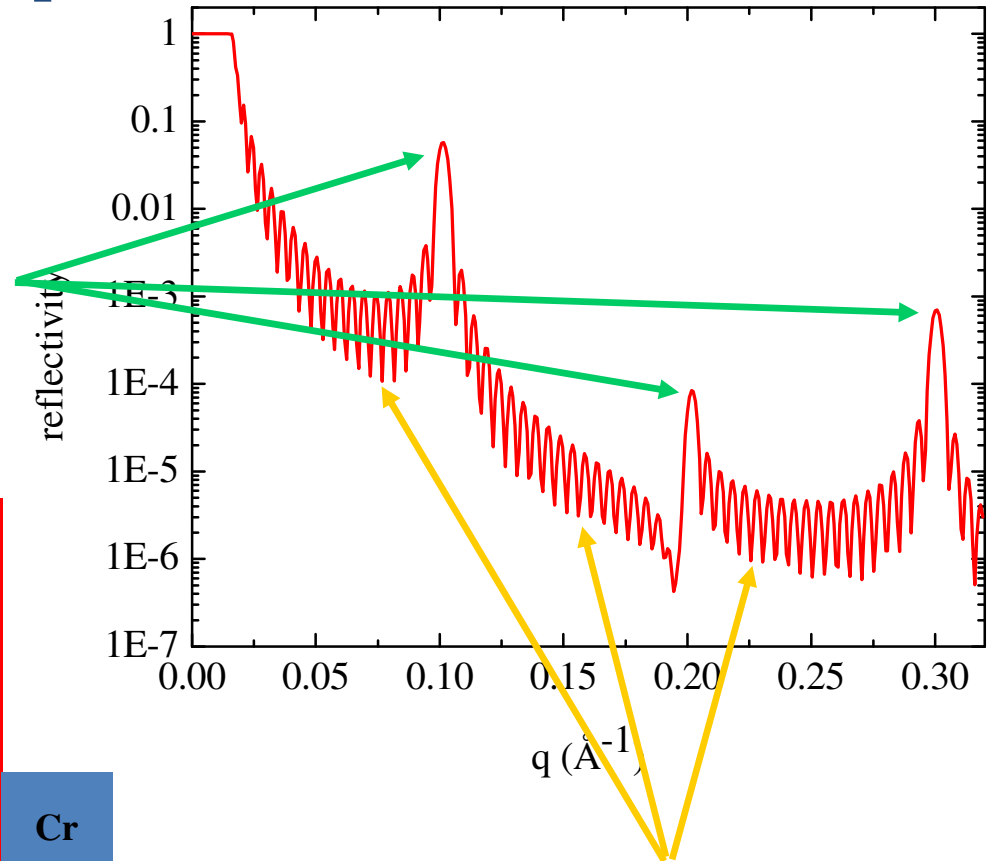
# Multilayer Bragg peaks

bilayer Bragg peaks at  $q=2\pi/t$

$$q = n \cdot 2\pi/62.8 \text{ \AA}^{-1} = n \cdot 0.1 \text{ \AA}^{-1}$$



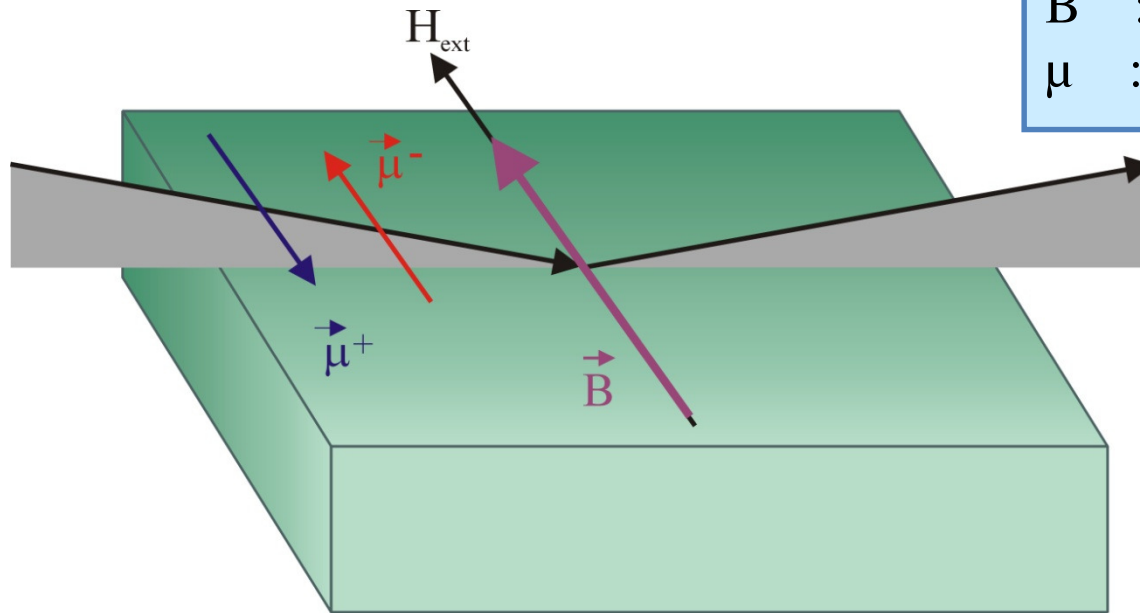
Bilayer thickness  $t$   
 $t = 32.8 \text{ \AA} + 30 \text{ \AA} = 62.8 \text{ \AA}$   
In total: 20 repetitions



Short period oscillations:  
Kiessig fringes

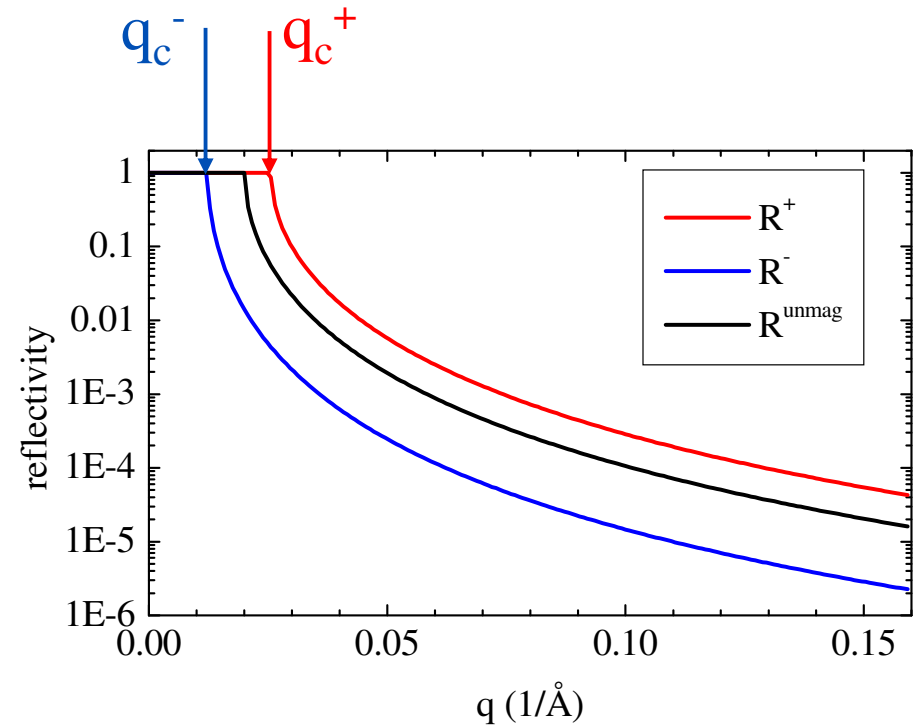
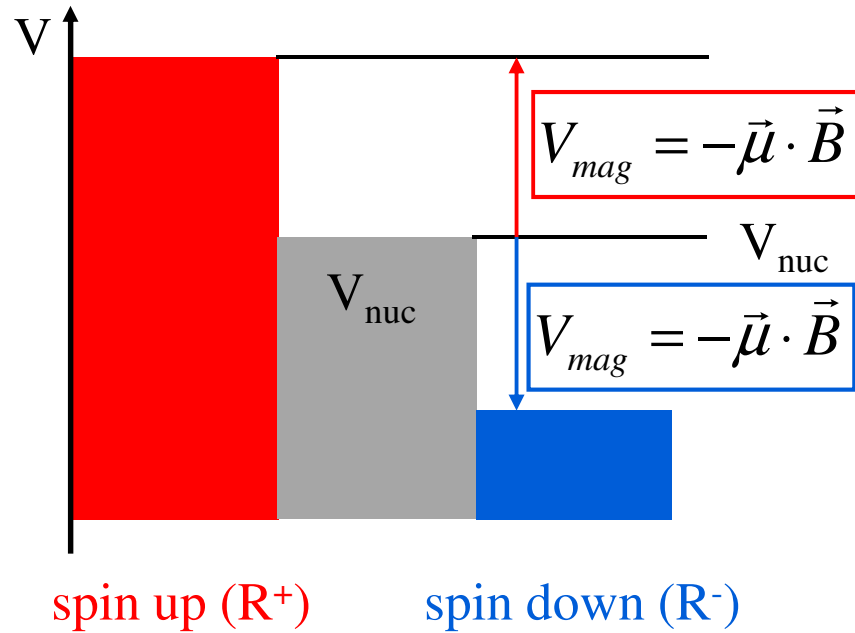
# Magnetic interaction

$H_{\text{ext}}$  : external magnetic field  
 $B$  : magnetic induction  
 $\mu$  : magnetic moment of neutrons



$$V = V_{nuc} + V_{mag} = \frac{2\pi\hbar^2}{m} \rho b - \vec{\mu} \vec{B} = \frac{2\pi\hbar^2}{m} \rho (b_{nuc} \pm b_{mag})$$

# PNR: bulk Fe

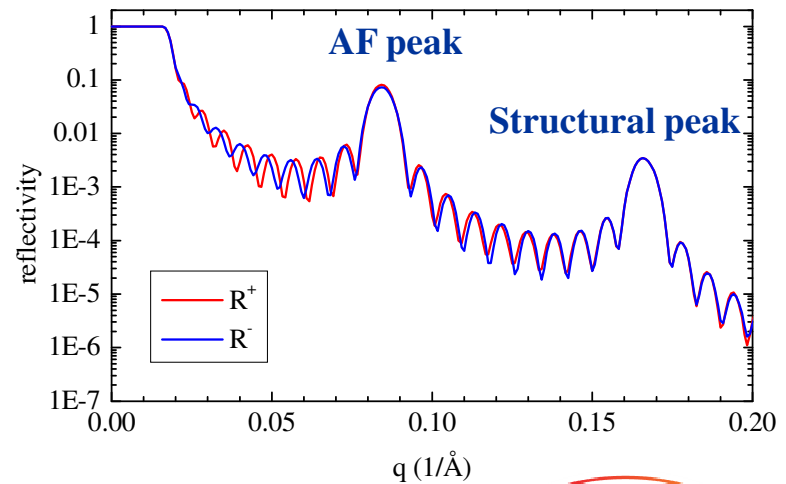
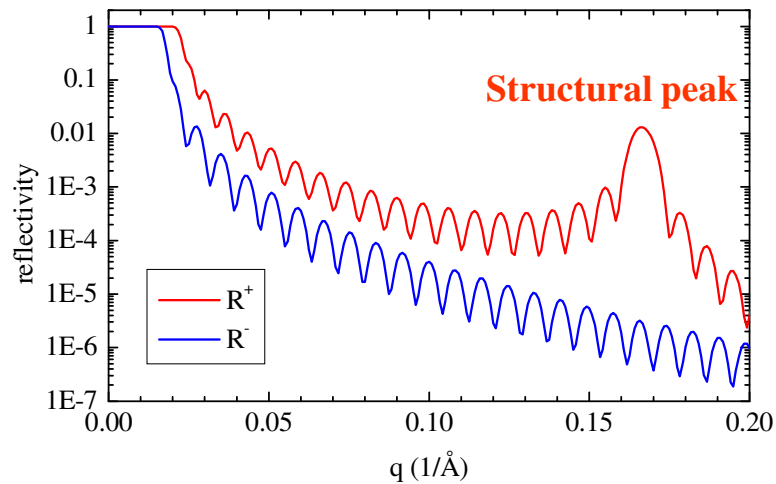
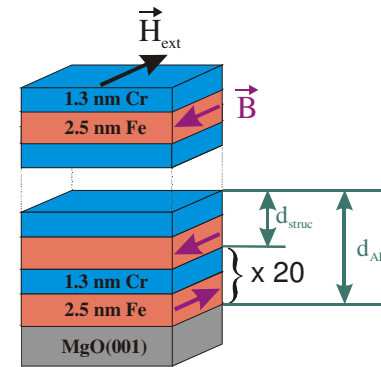
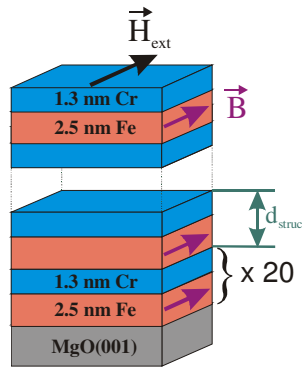


Different reflectivity for spin-up and spin-down neutrons  
 $\Rightarrow$  Determination of the absolute magnetic moment possible

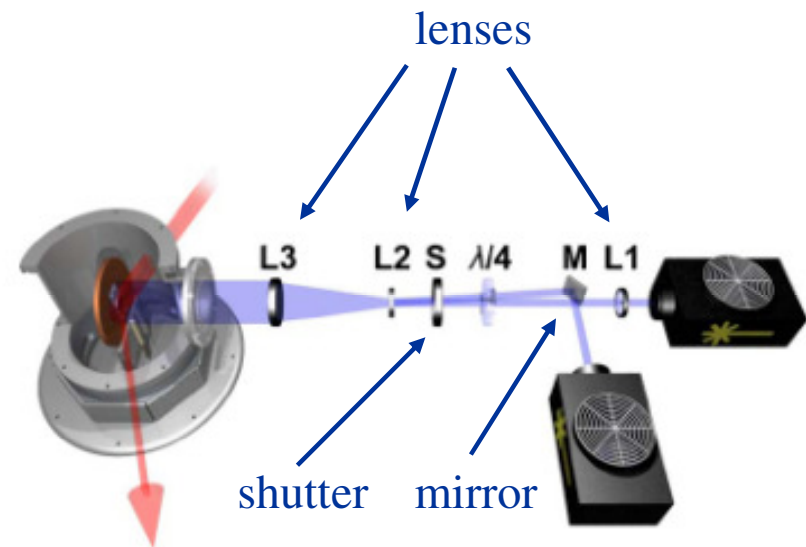
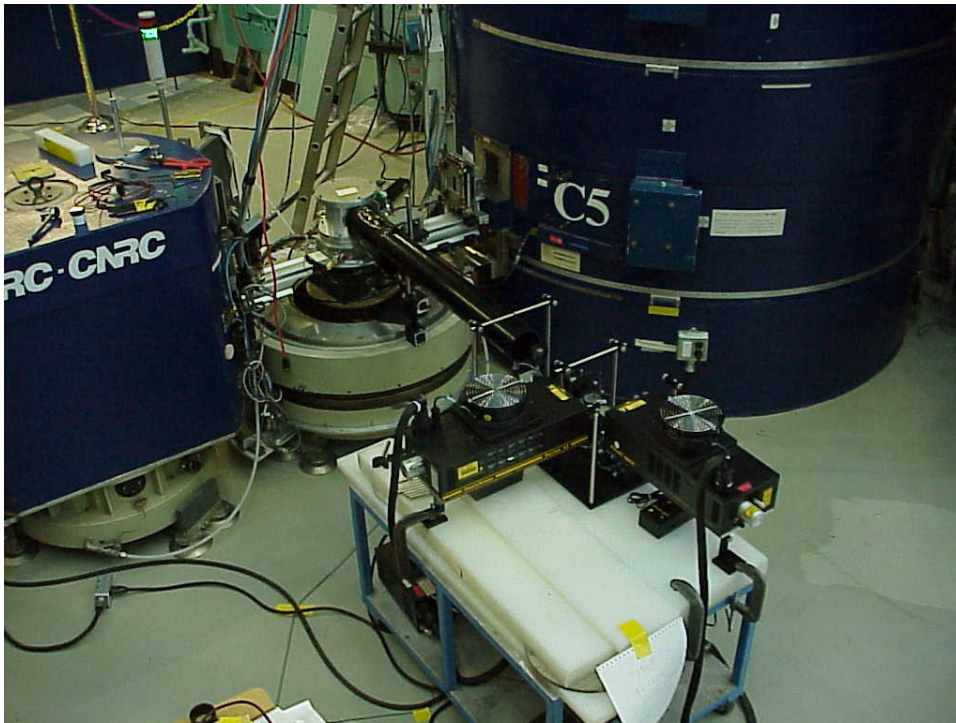
# PNR: Fe/Cr multilayers

Ferromagnetic coupling:  
Magnetic period = chemical period

Antiferromagnetic coupling:  
Magnetic period = 2 x chemical period

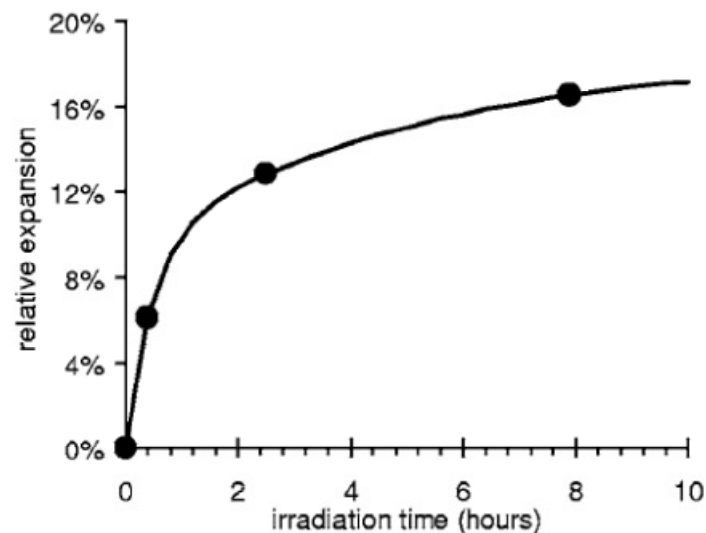
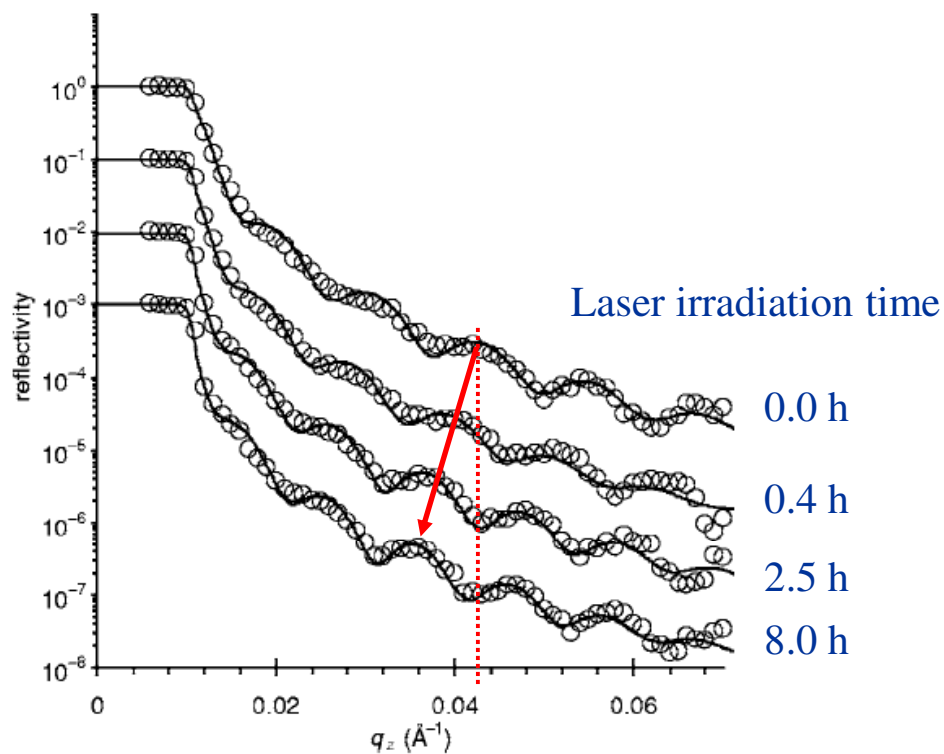


# In-situ setup for photoactive films



Neutron reflectometry and Laser illumination at the same time

# Results for azobenzene films



Smaller  $\Delta q \Rightarrow$  larger film thickness

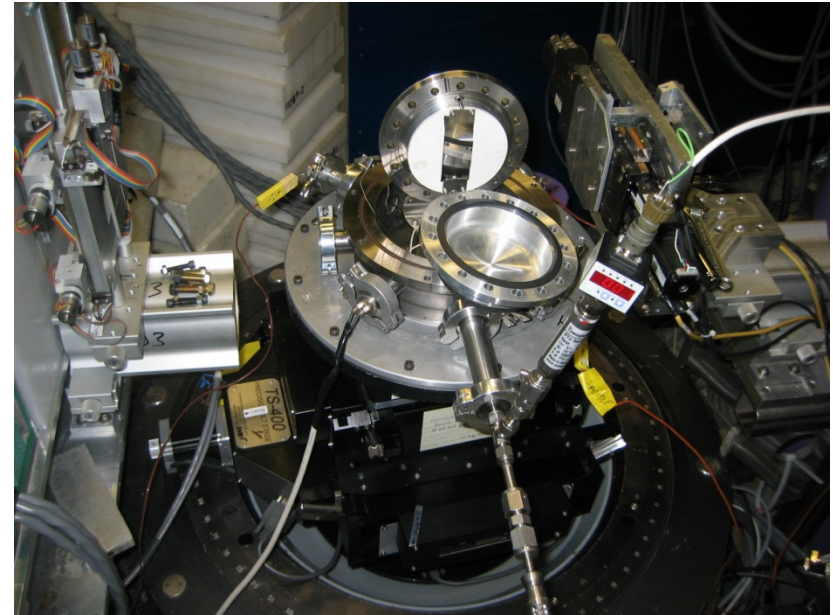
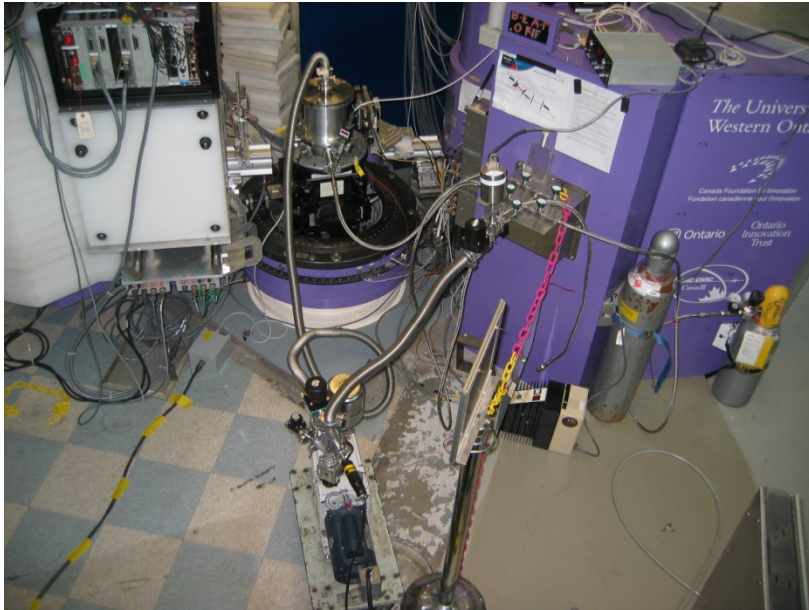
K. Yager, O. M. Tanchak, C. Godbout, H. Fritzsche, and C. Barrett  
*Photomechanical effects in azo-polymers studied by neutron reflectometry*  
Macromolecules **39**, 9311 (2006); citations: 42

# From summer school to real experiments in 2 months



Kevin Yager, Oleh Tanchak:  
Neutron summer school: June 2004  
First experiments: August 2004

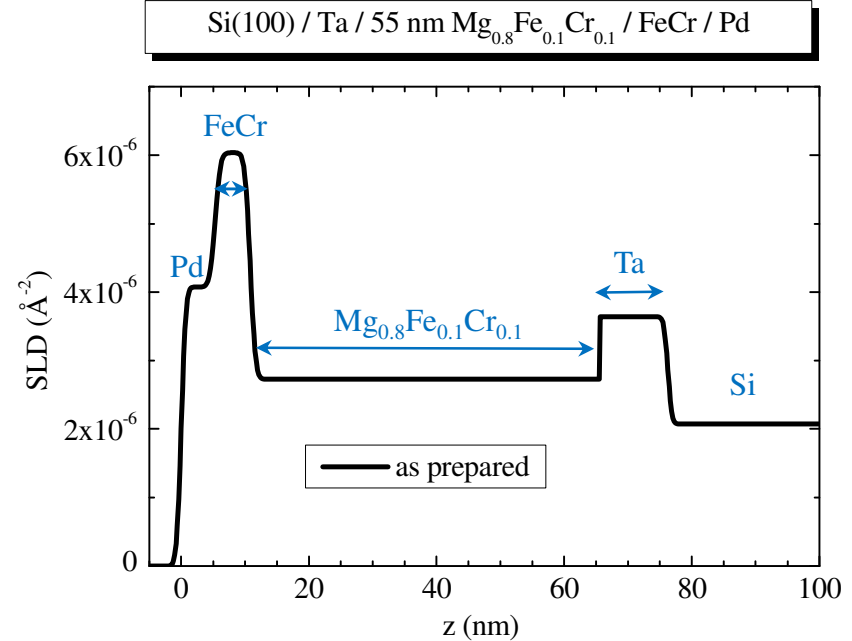
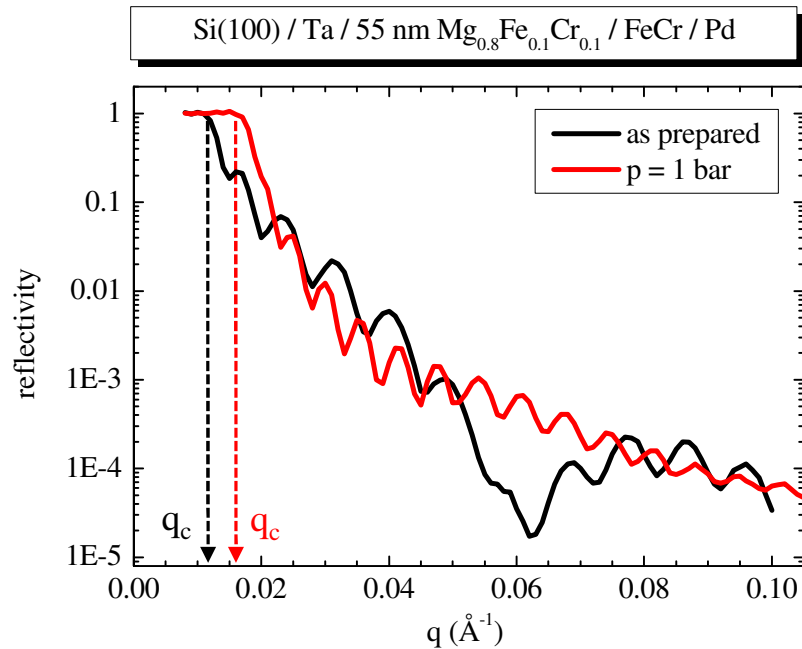
# sample cell for hydrogen absorption



In-situ hydrogen absorption:  
Up to 400° C, 40 bar

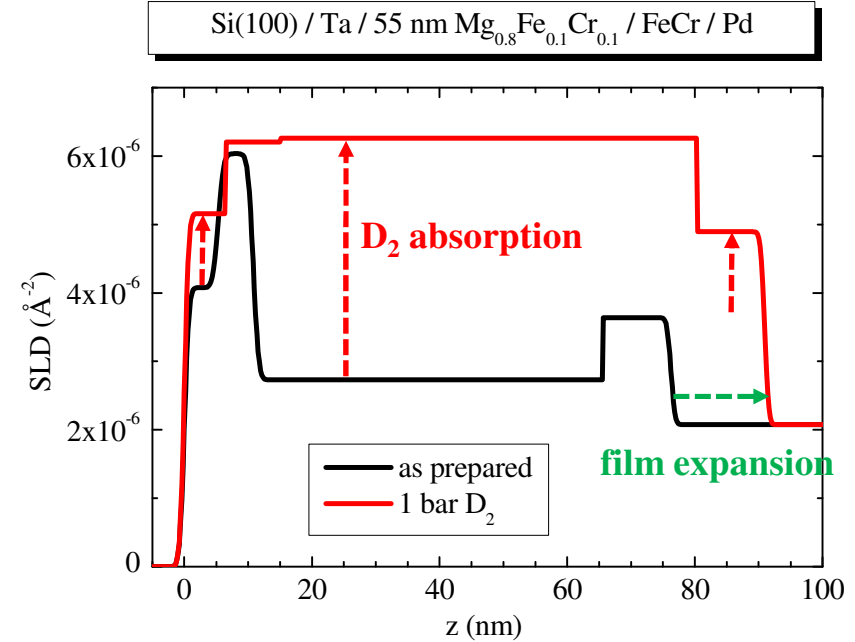
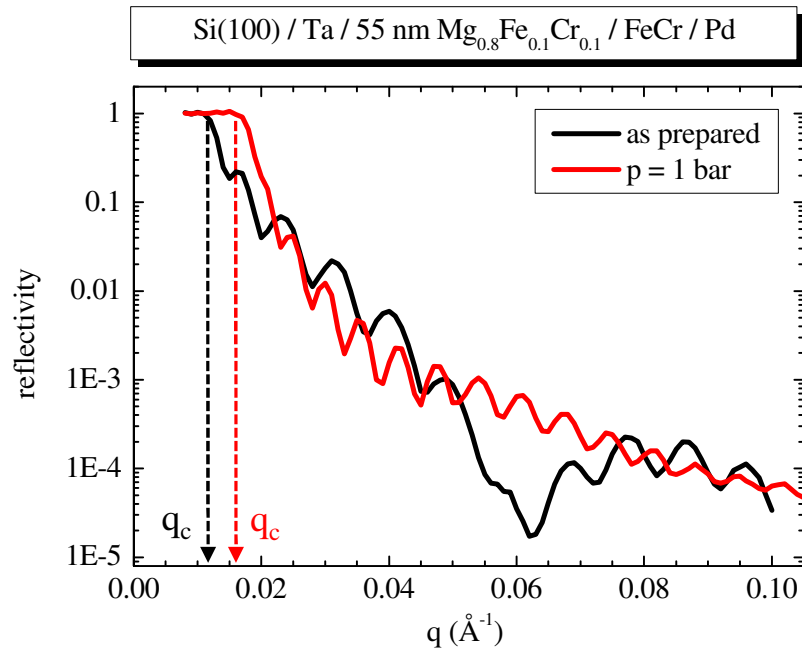


# Deuterium absorption at RT



- i)  $q_c$  increases upon  $\text{D}_2$  absorption  $\Rightarrow$  MgFeCr is absorbing  $\text{D}_2$
- ii) The frequency of the Kiessig oscillation increases  $\Rightarrow$  film is expanding

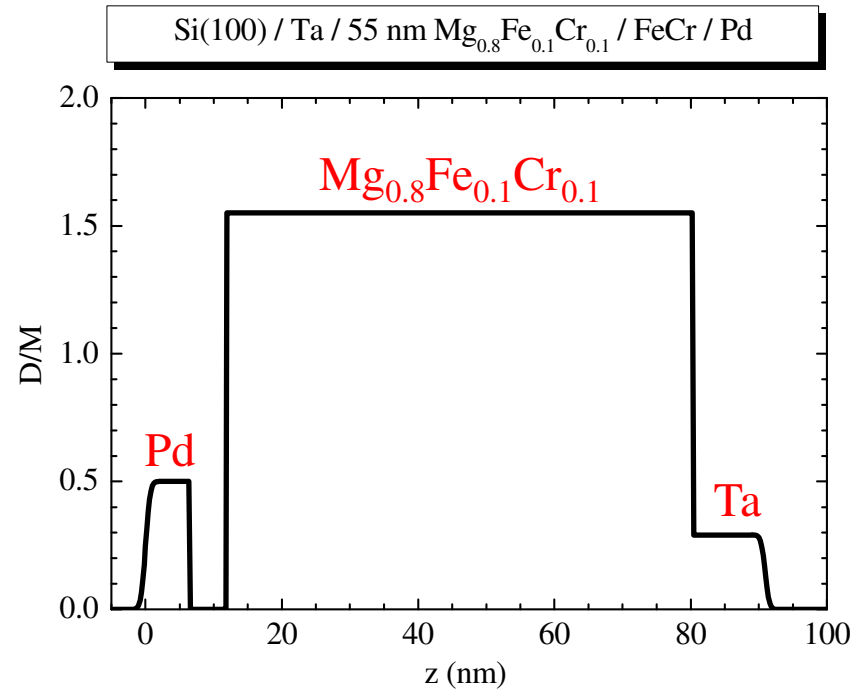
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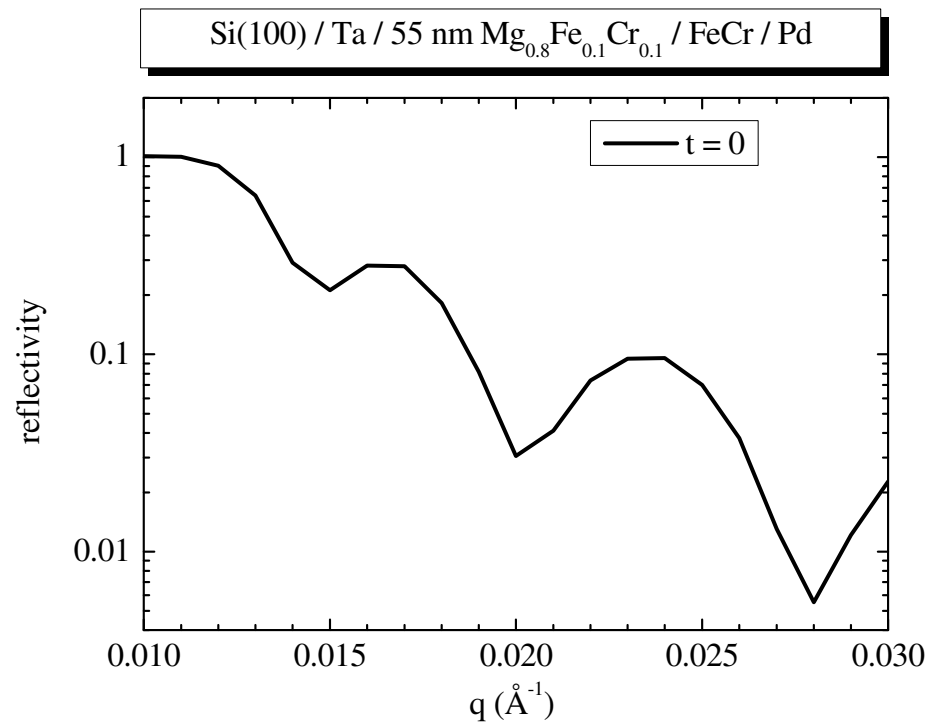
# Deuterium concentration profile

$$c_{deut} = \left( \frac{SLD_{deut}}{SLD_M} \cdot \frac{t_{deut}}{t_M} - 1 \right) \frac{b_M}{b_D}$$

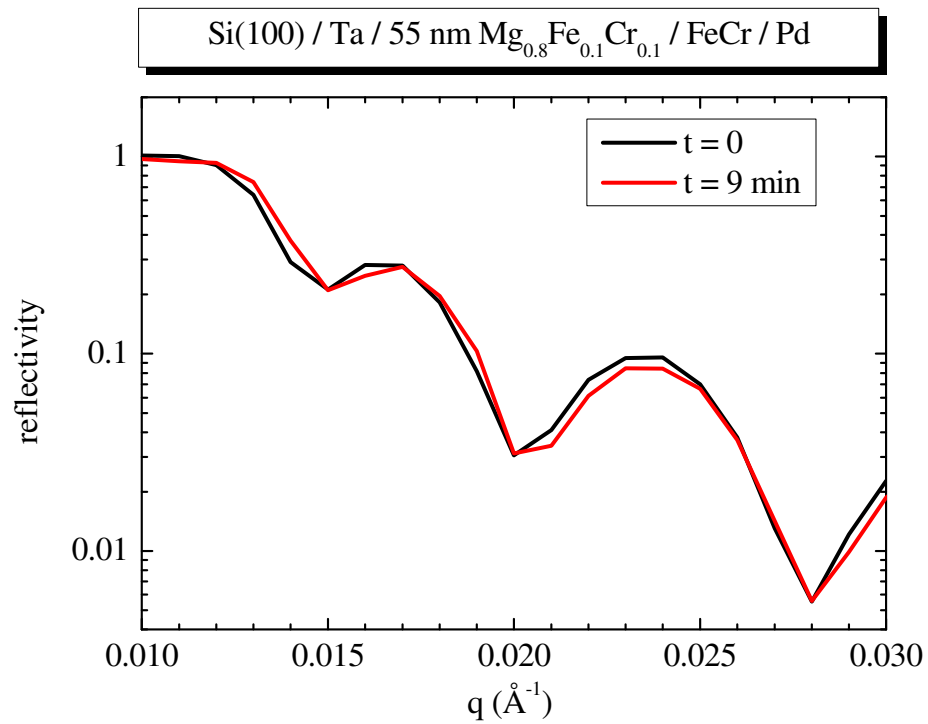


- Absorption in  $Mg_{0.8}Fe_{0.1}Cr_{0.1}$  up to  $D/M=1.55$  (almost all Mg reacts to  $MgD_2$ )
- Film expands by 20%

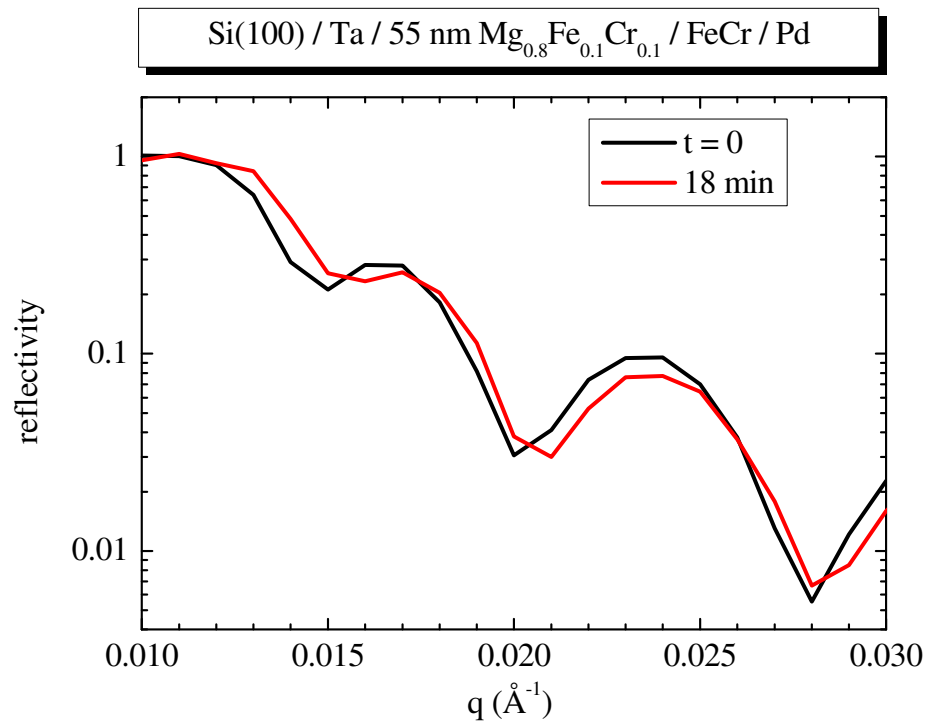
# Kinetics at RT and 8 mbar D<sub>2</sub>: The reflectivity curve



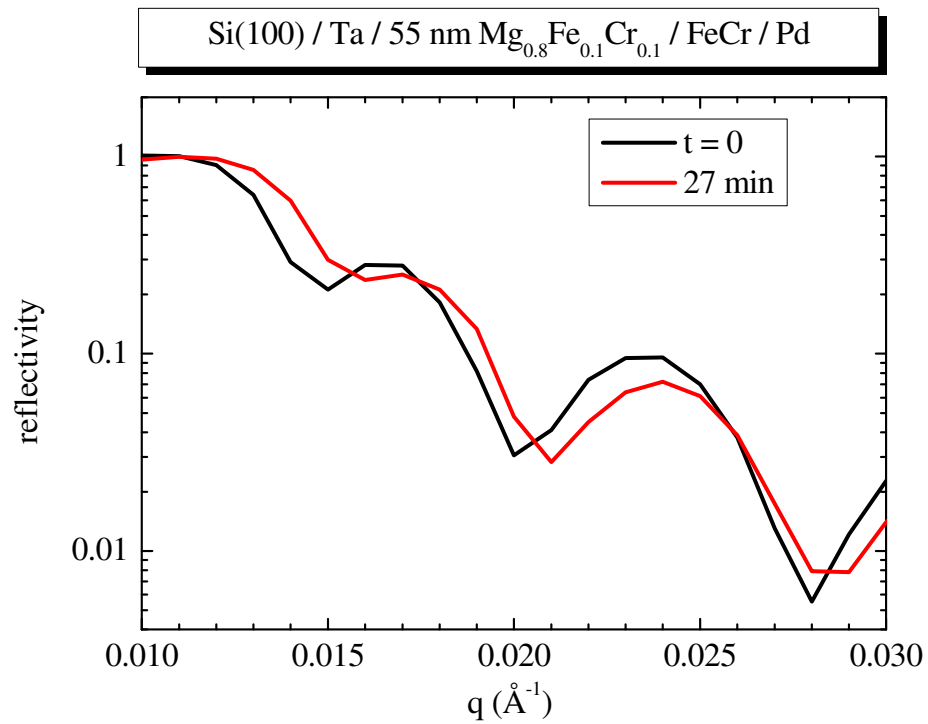
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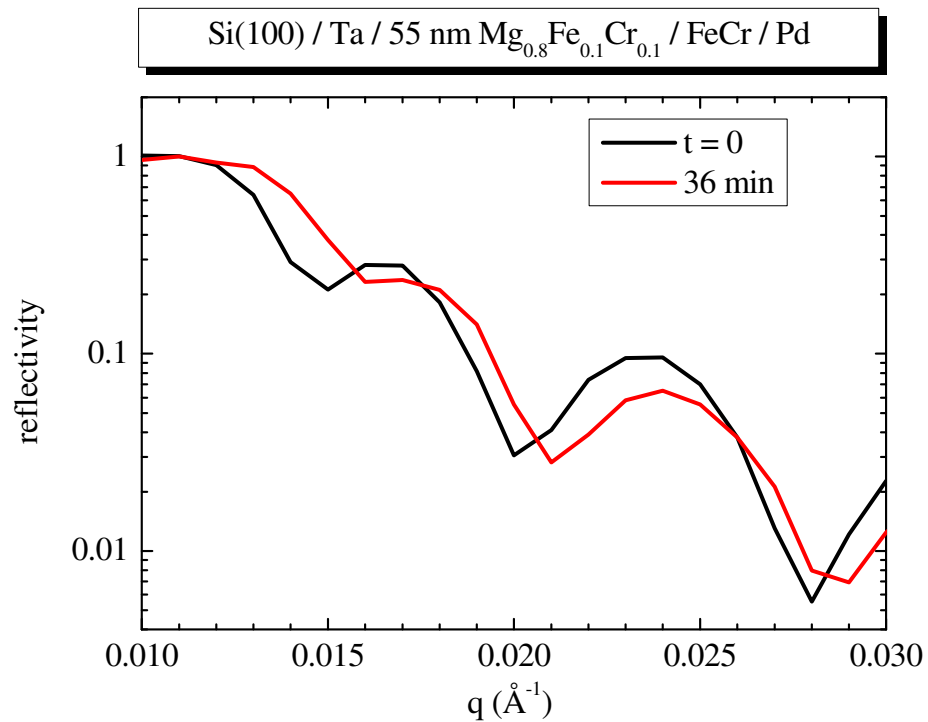
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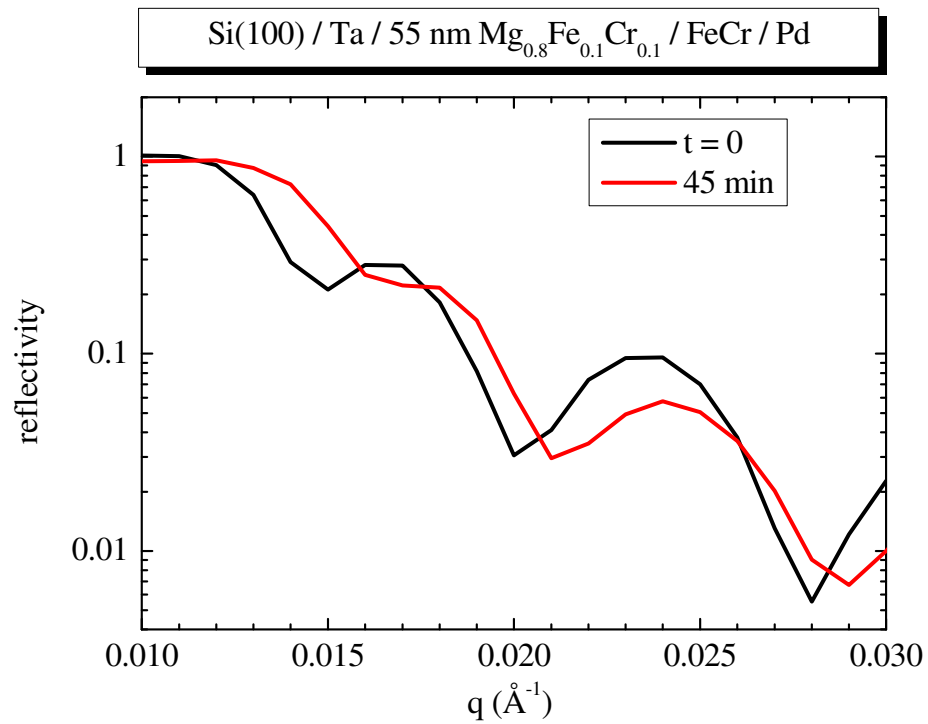


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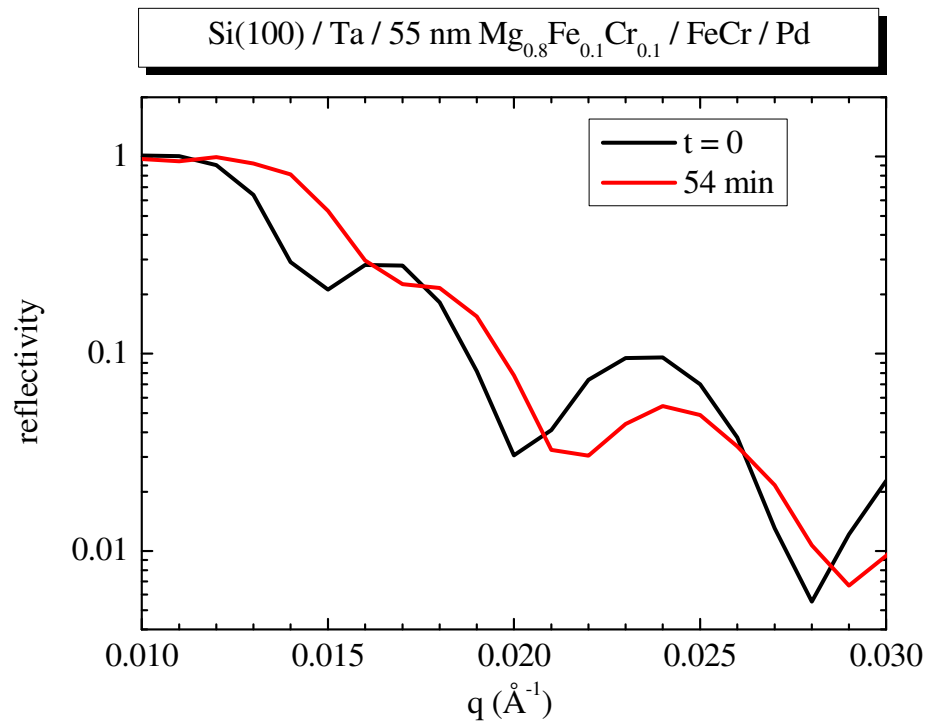




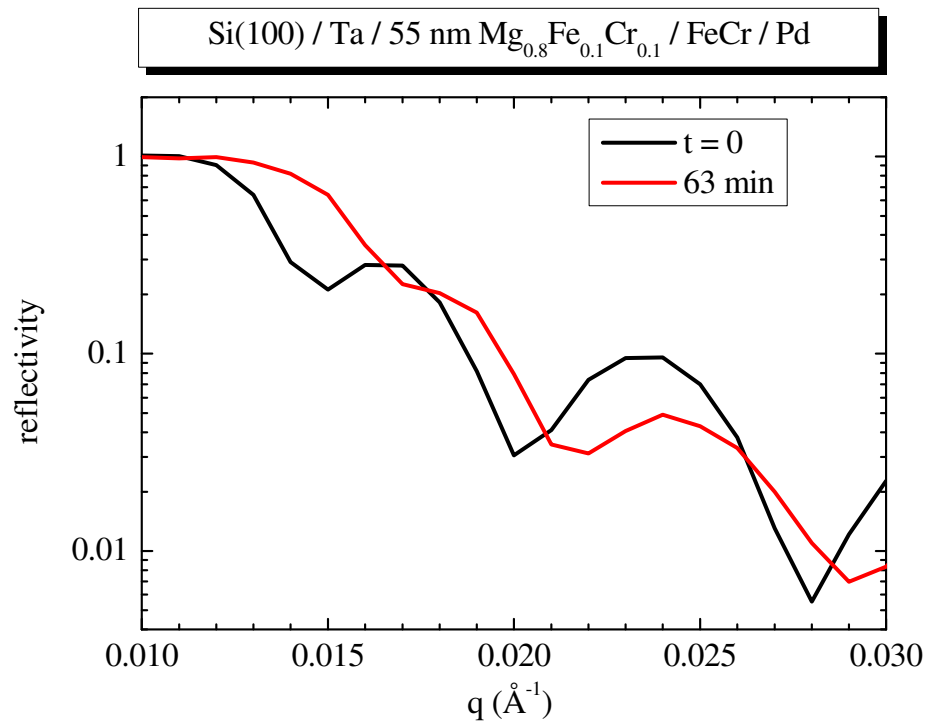
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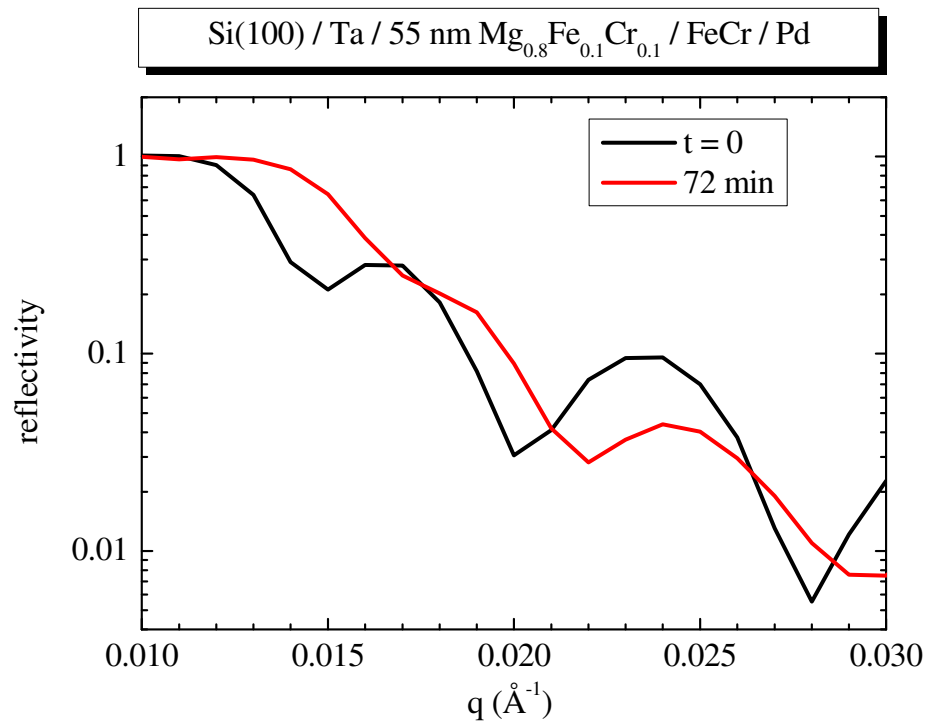
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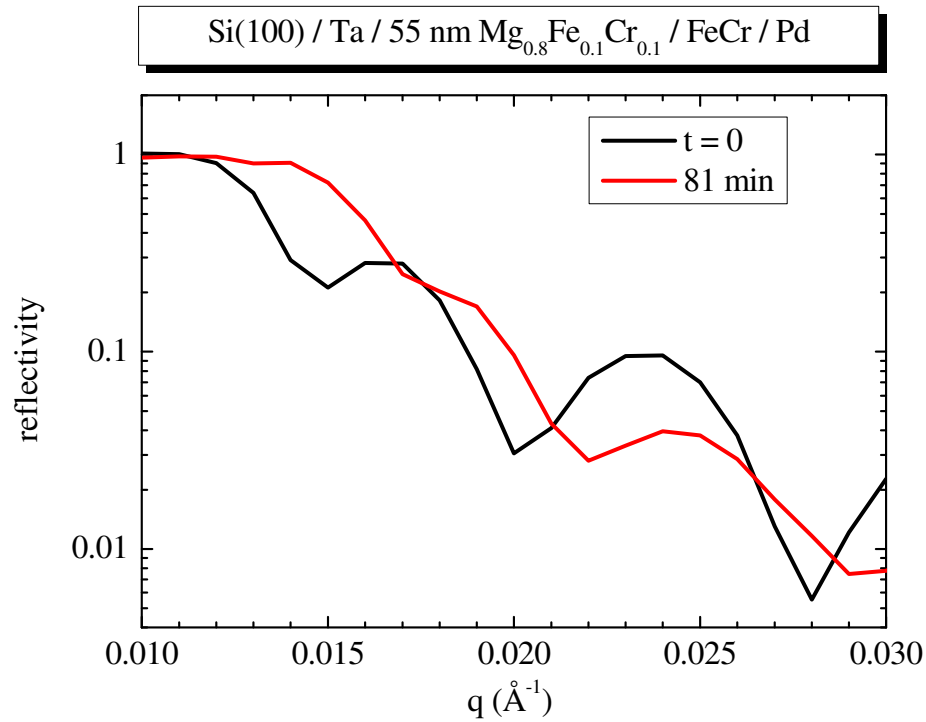
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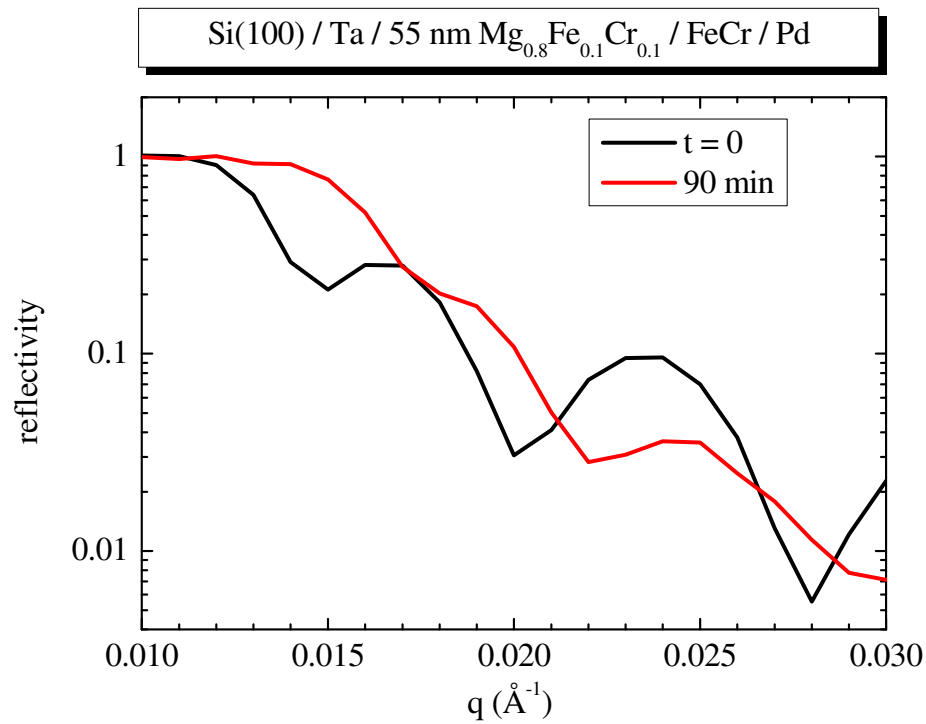
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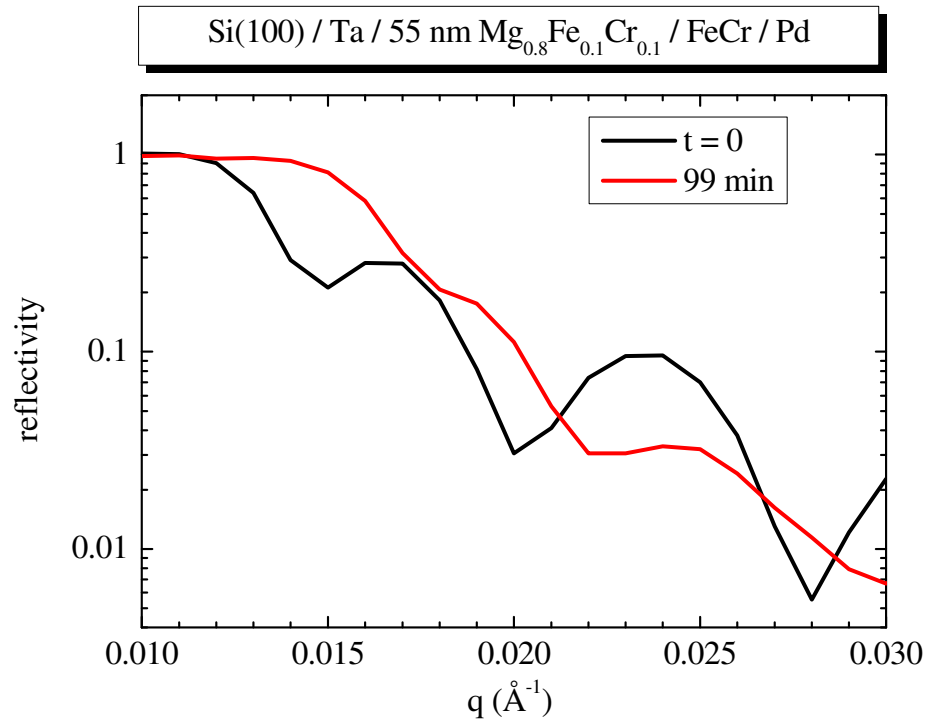
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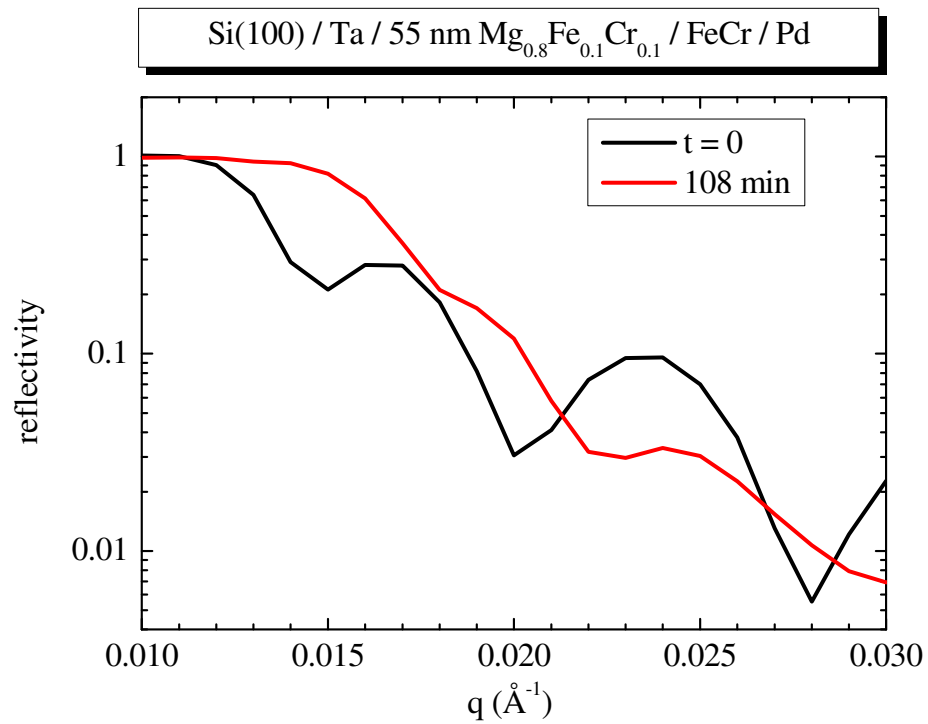
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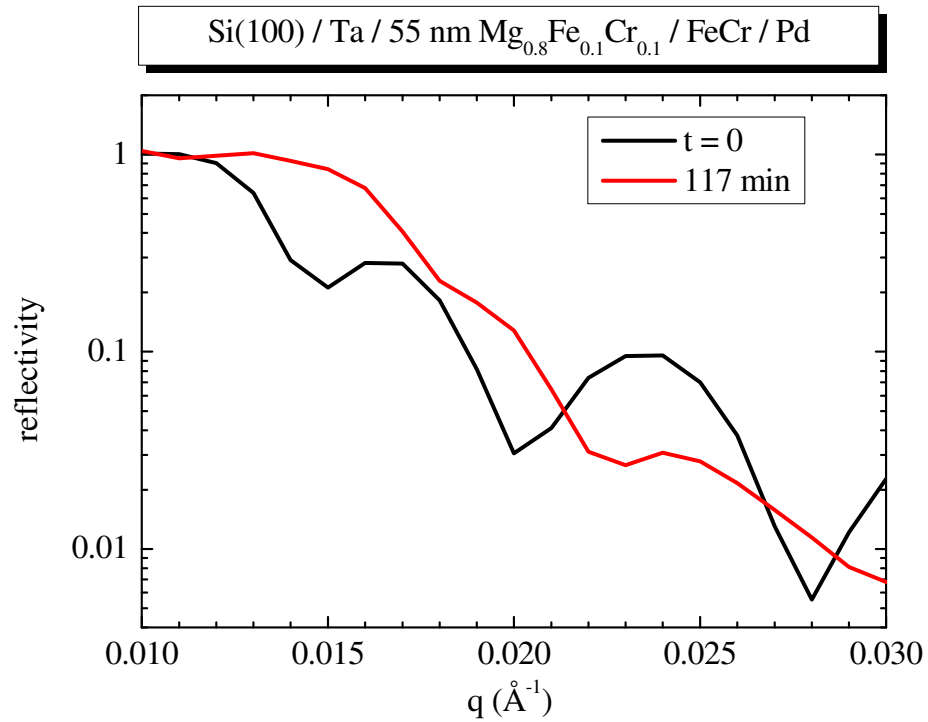


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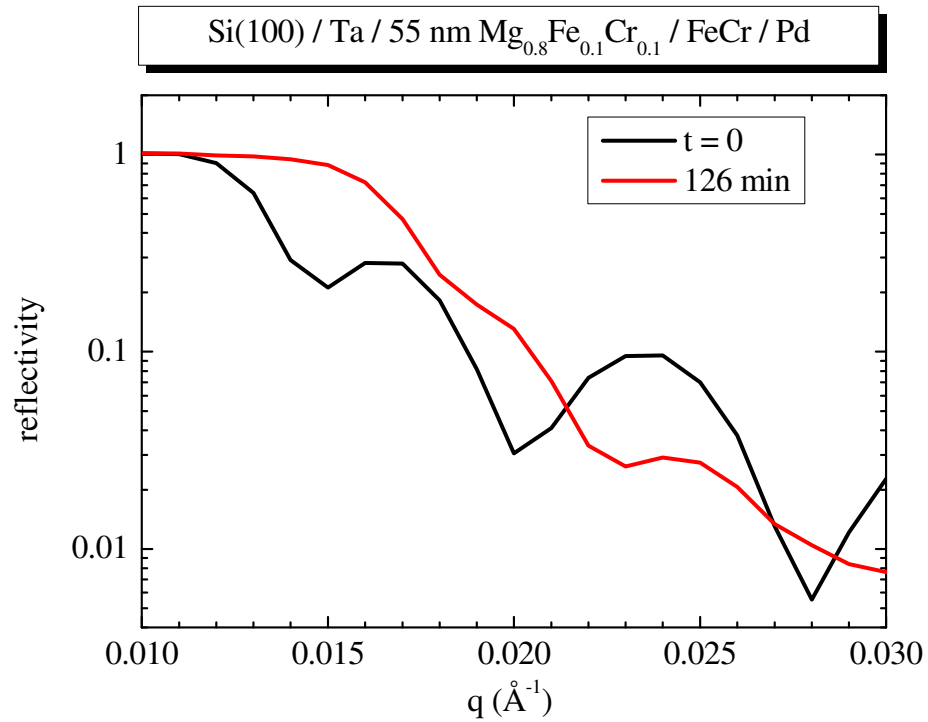




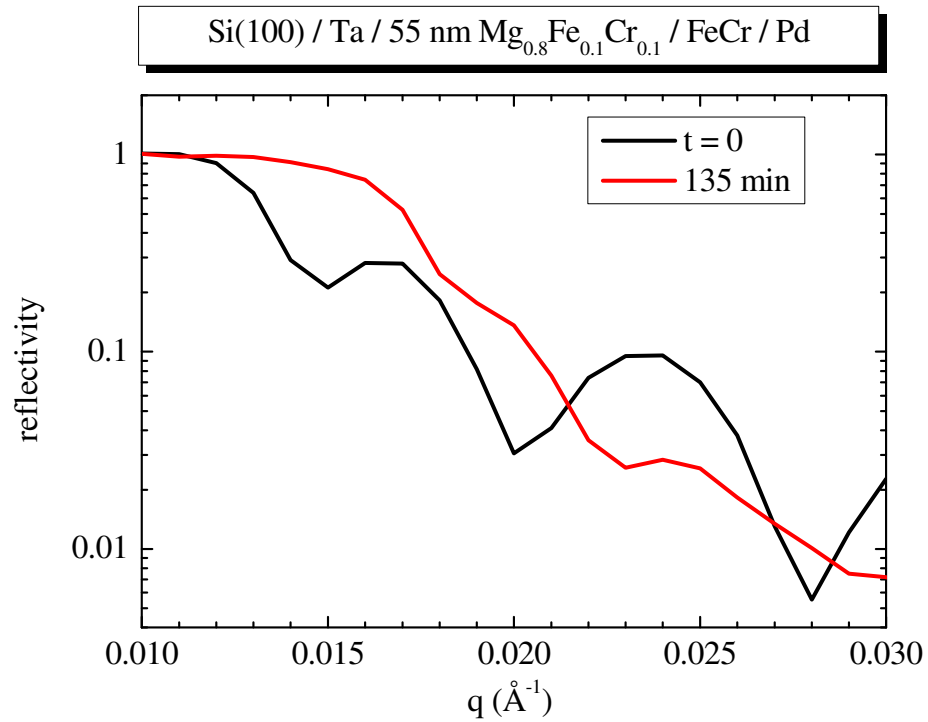
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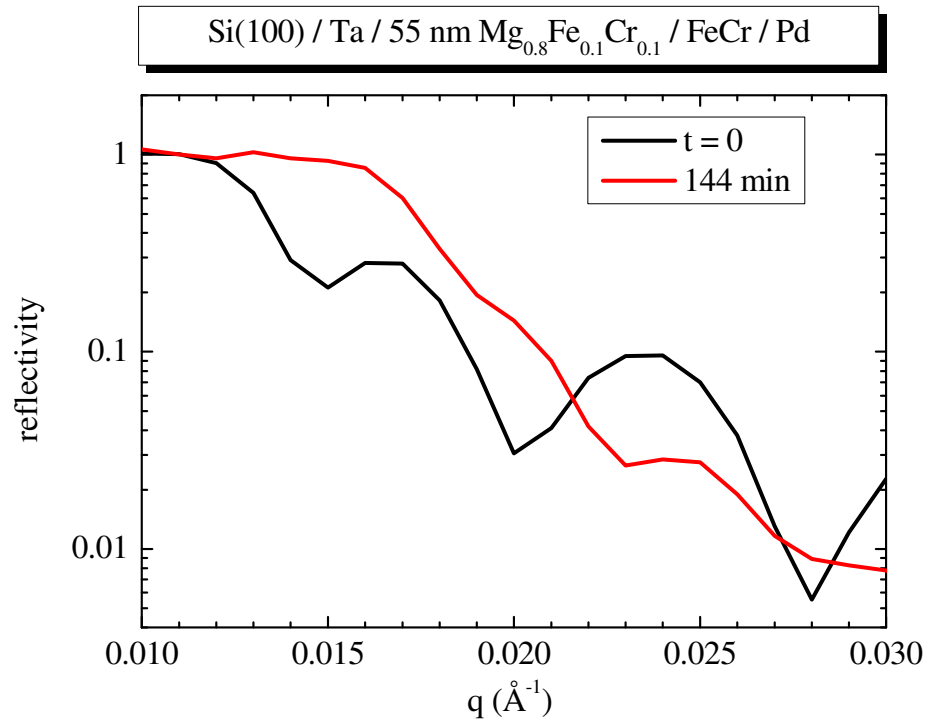
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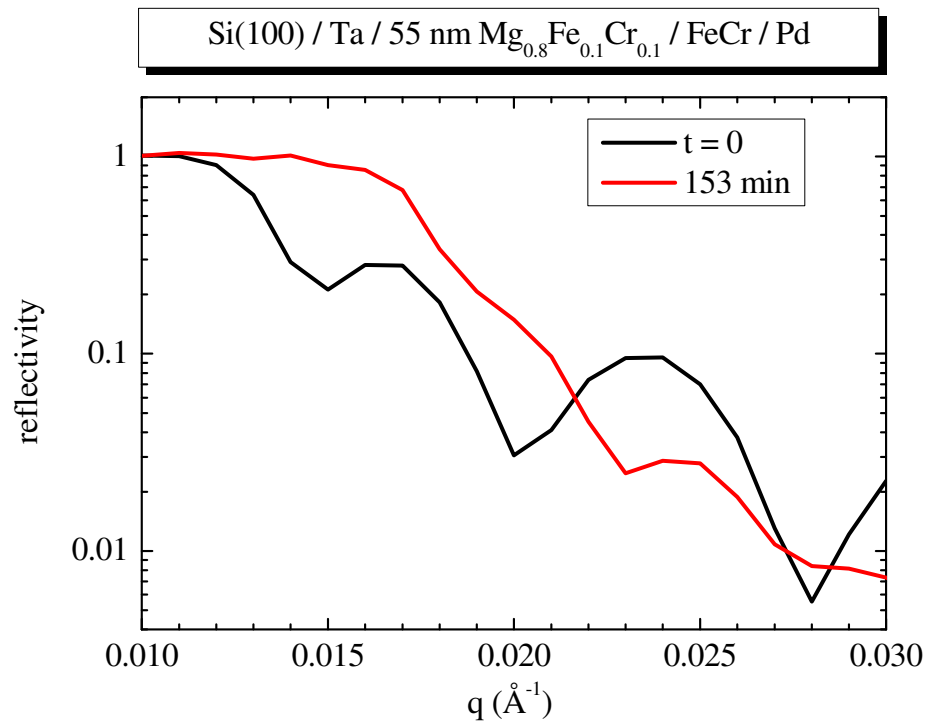
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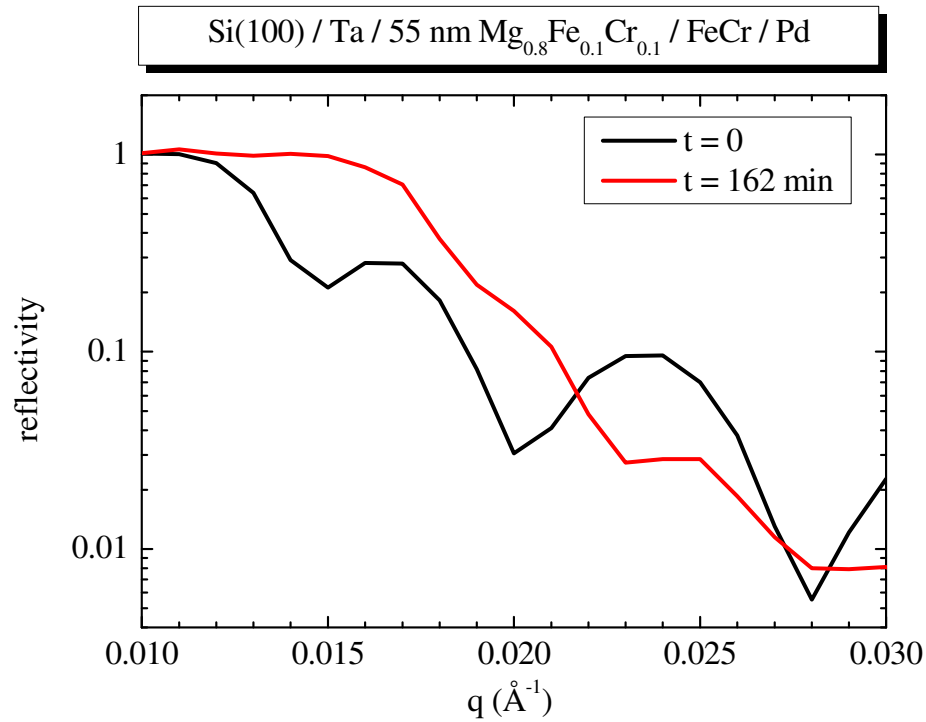
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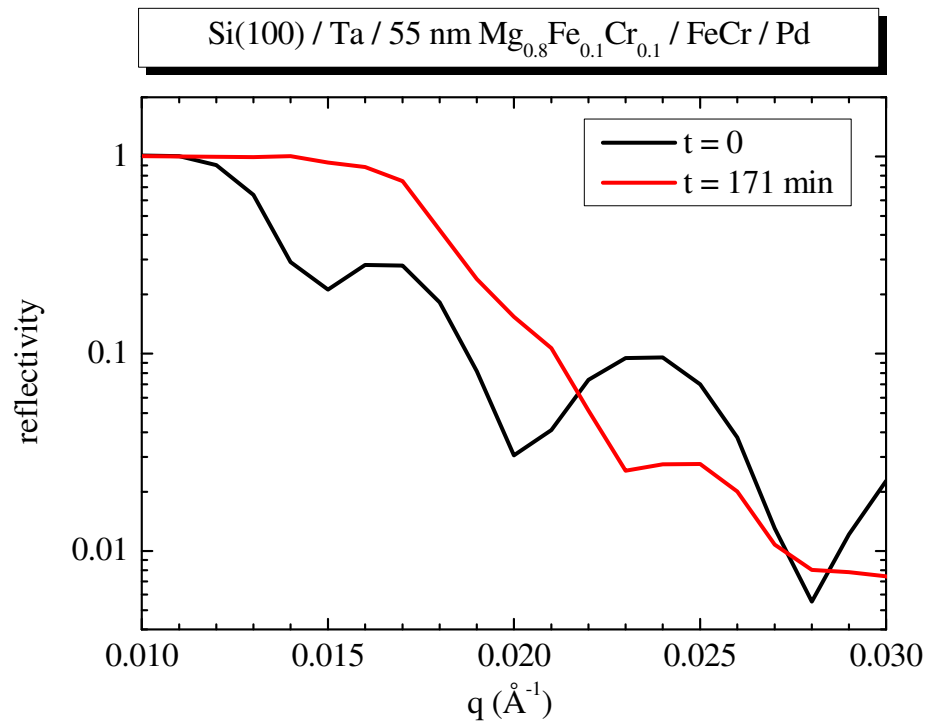
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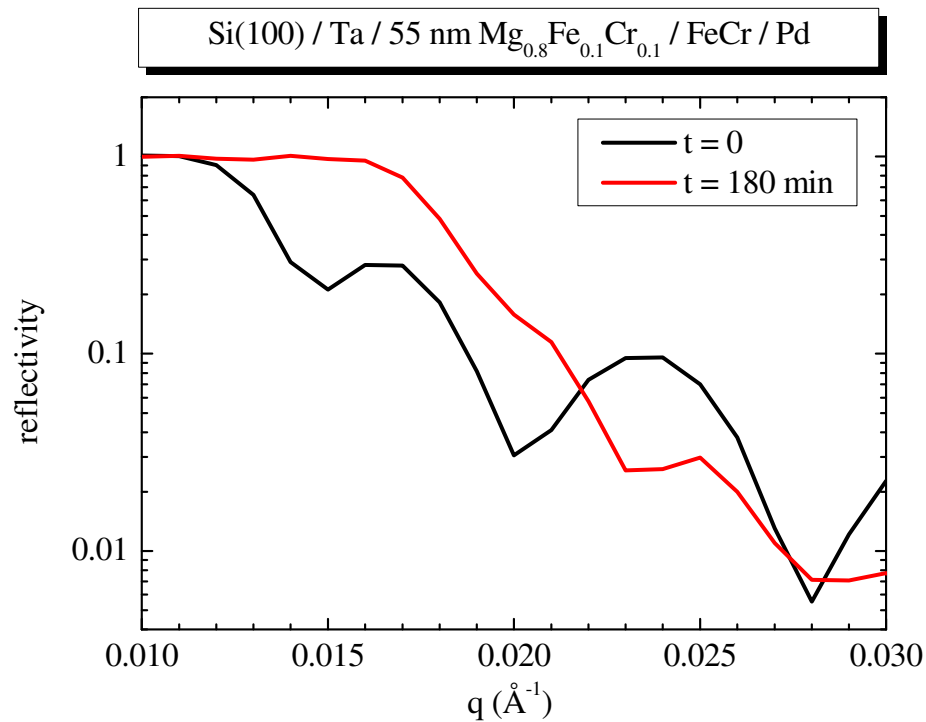
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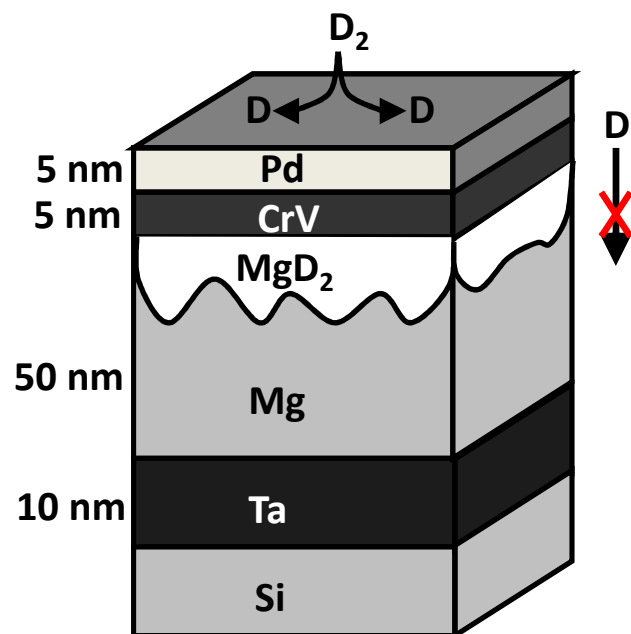


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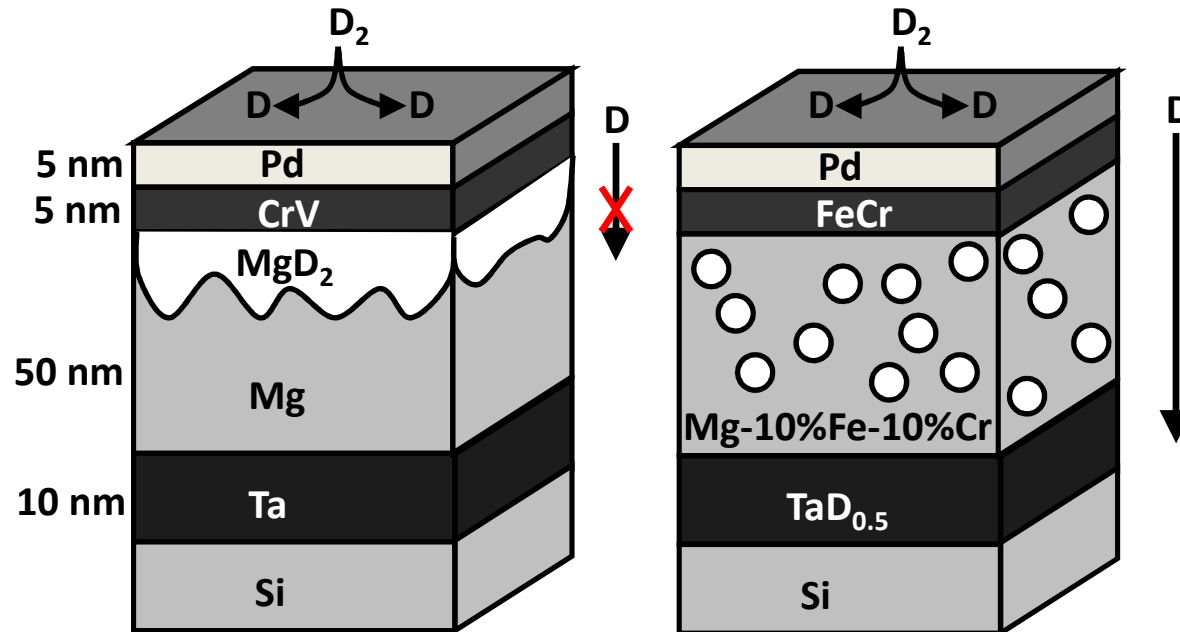
# Mg vs. MgFeCr: different mechanisms



Mg: formation of blocking MgD<sub>2</sub> layer

P. Kalisvaart, E. Luber, H. Fritzsche, D. Mitlin, Chem. Commun. **47**, 4294 (2011)

# Mg vs. MgFeCr: different mechanisms



Mg: formation of blocking  $\text{MgD}_2$  layer

Fe and Cr segregation leads to:

- many nucleation sites
- homogeneous hydrogenation

H. Fritzsche, W. P. Kalisvaart, B. Zahiri, R. Flacau, and D. Mitlin, Int. J. Hyd. Energy **37**, 3540 (2012)

# supermirror

**goal:**

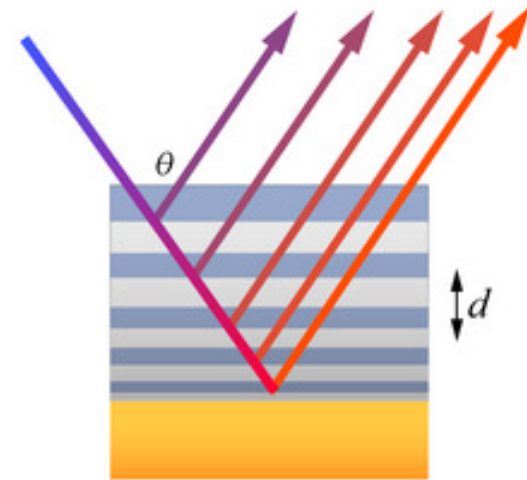
Extend the range of neutron reflection beyond the regime of total reflection

**concept:**

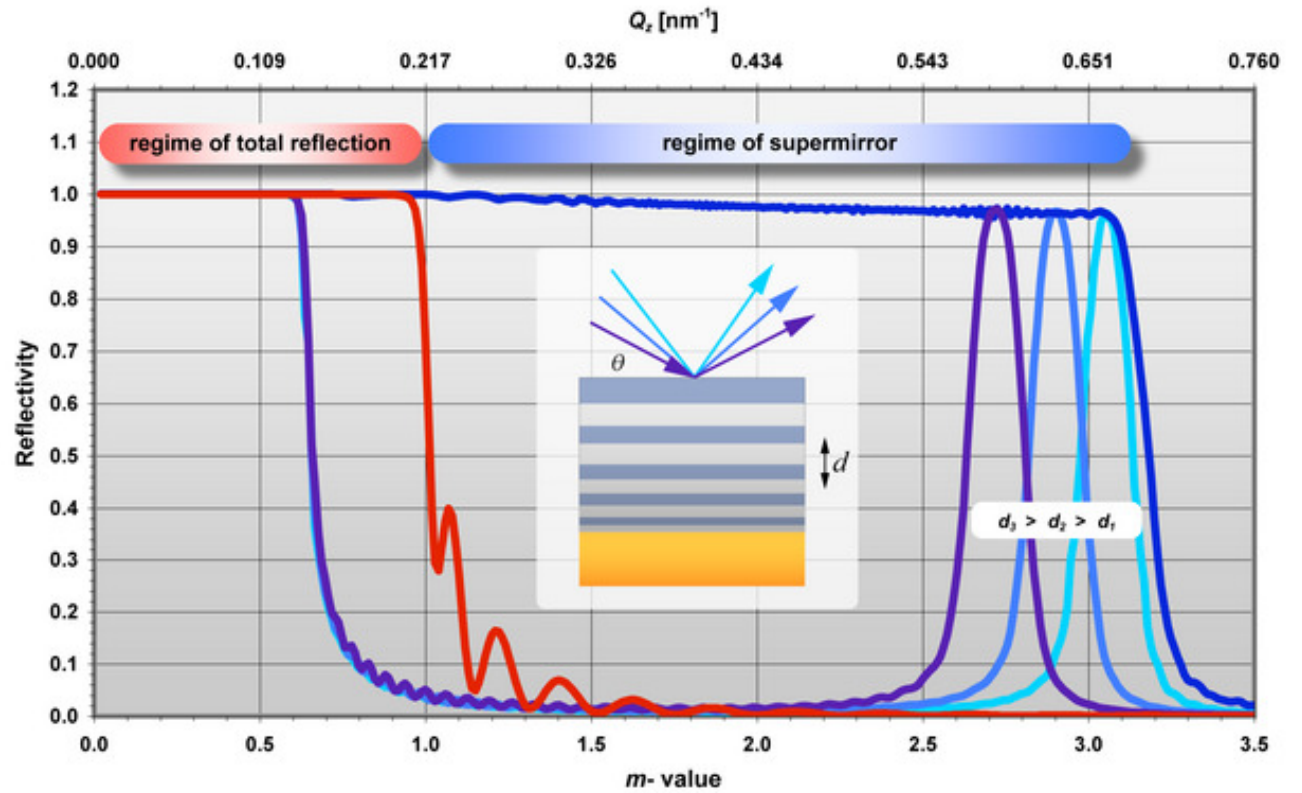
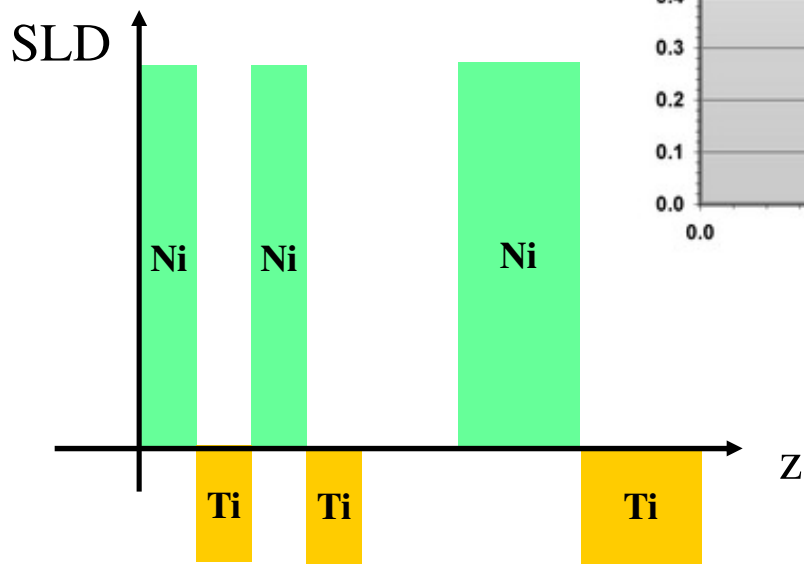
continuous Bragg reflection from a multilayer composed of bilayers with a variation of the thickness

**realization:**

Ni/Ti multilayer,  $b_{\text{Ni}} = 10.3 \text{ fm}$ ,  $b_{\text{Ti}} = -3.4 \text{ fm}$   
100 bilayers,  
 $q_c = 2 \times q_{c, \text{Ni}}$



# supermirror



**m-value:**  $m = q_c / q_{c, \text{Ni}}$

# Polarizing supermirror

**concept:**

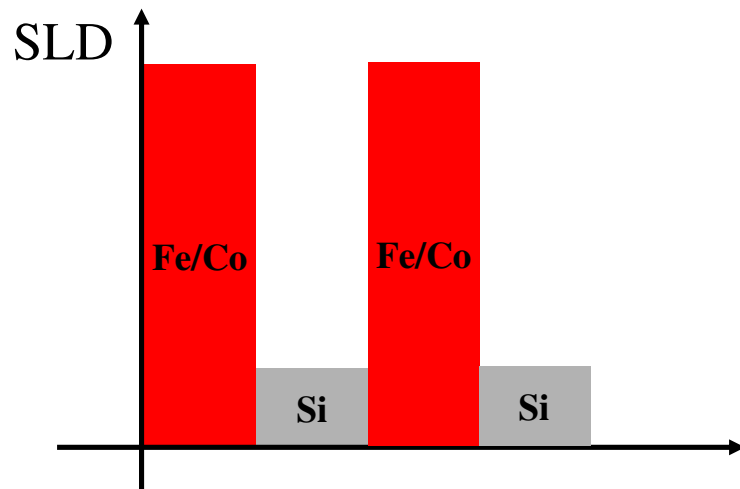
Using the supermirror concept with a magnetic/non-magnetic bilayer

The SLD of the bilayer is index-matched for spin-down neutrons

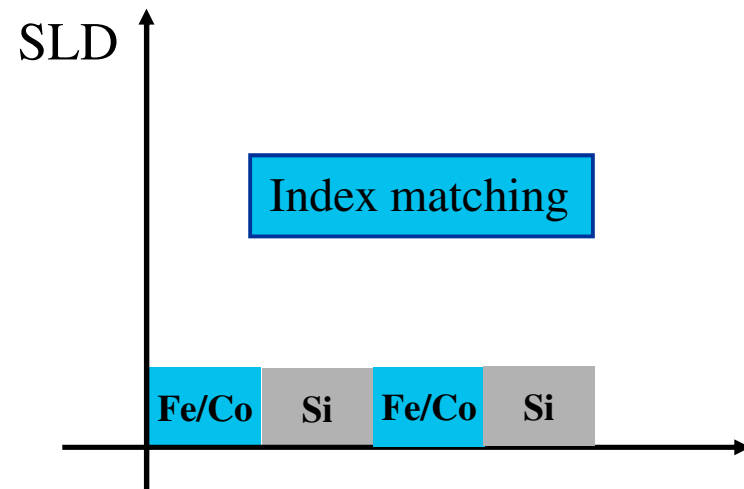
no multilayer Bragg peaks for down-neutrons

Spin-up neutrons show supermirror behavior with extended critical edge

spin-up neutrons

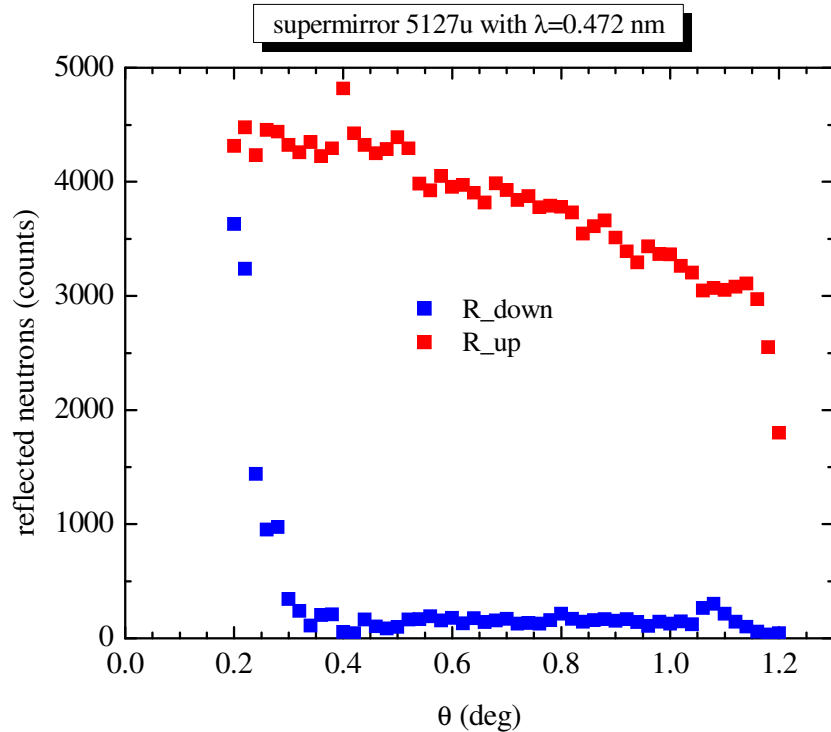


spin-down neutrons

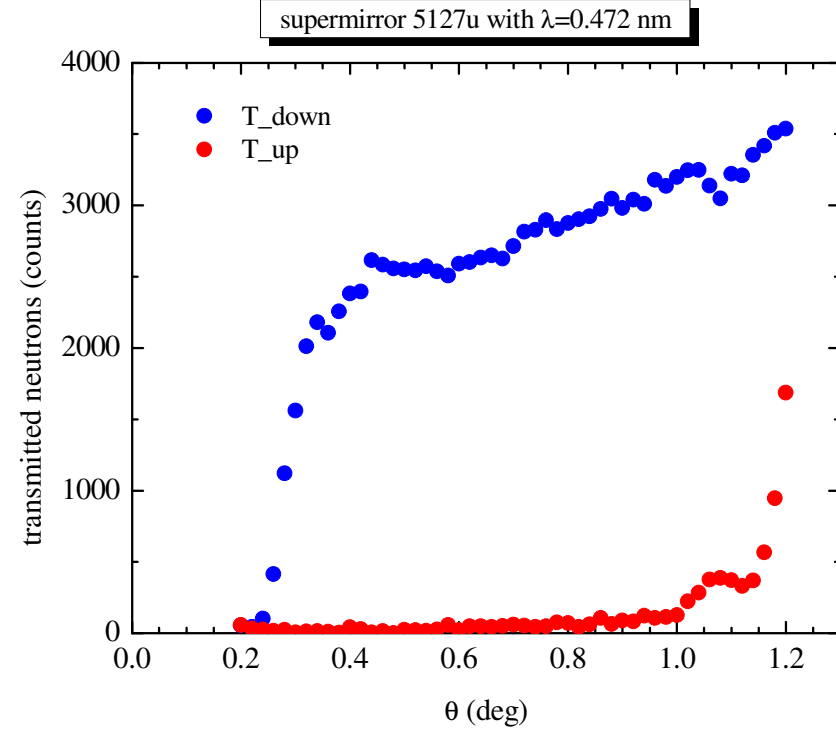


# Fe-Co/Si polarizing supermirror

Reflected intensity

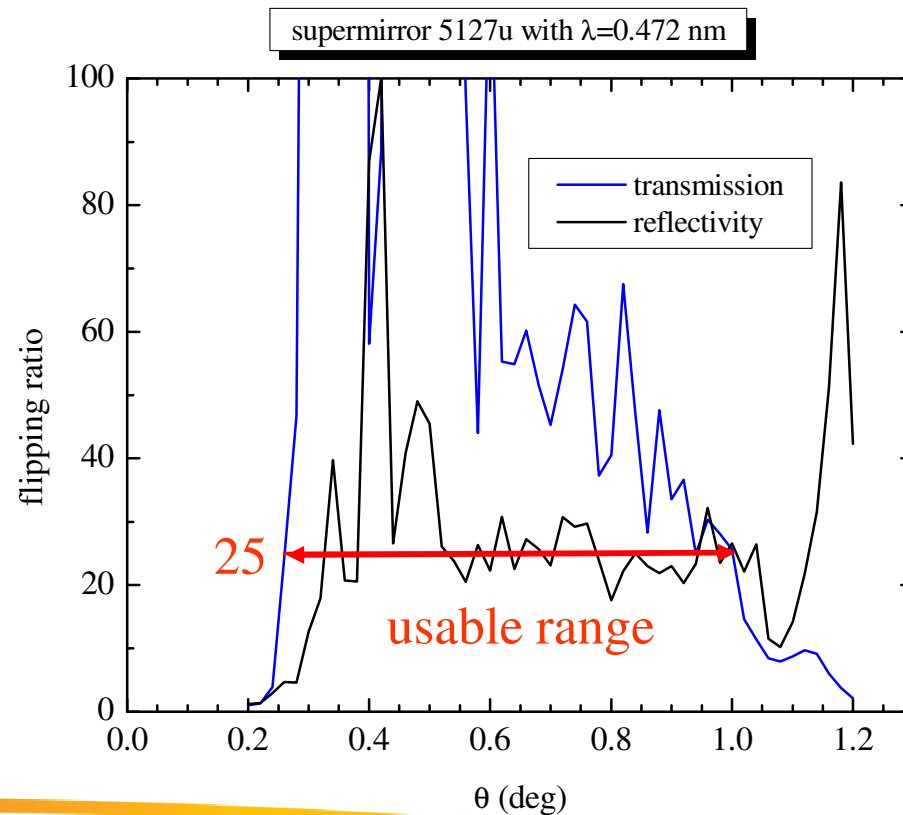


Transmitted intensity



# Supermirror: flipping ratio

$$\text{Flipping ratio} = \frac{R^+ - R^-}{R^+ + R^-}$$





# Discussion

Thank-you



National Research  
Council Canada

Conseil national  
de recherches Canada

Canada